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Derivation of the Generalized, Average Euclidean Distance Function for the PDI Model

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PREFACE

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A handwritten signature in dark ink, appearing to read 'P. A. La Brecque', is positioned above the printed name.

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13. ABSTRACT (Maximum 200 words) This report derives distance functions that form the basis for the Population Density Index (PDI) model, which is a three-parameter square-root model for measuring discrete spatial density in finite populations. The PDI and its methods have been applied to facilities layout methodologies in submarine environments at the Naval Undersea Warfare Center Division, Newport, RI, resulting in several U.S. patent applications. The emphasis here is on the "micro-population" model in which the linear units are "feet." The derivations relate Cartesian rectangular coordinate systems to uniform unit and nonunit lattices, as well as to the nonlattice distribution. Other proofs relate to the bounds of the calculated density measure and the density rate index called "effective distance." Alternative distance functions are discussed, and examples of the numerical calculations are provided. Also derived is the algorithm for selecting a rectangular lattice conformal to a quadrilateral area and for calculating interpoint distance in a PDI lattice. A table of computer-generated unit lattice average Euclidean distances for up to 10,000 density points is included.				
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DERIVATION OF THE GENERALIZED, AVERAGE EUCLIDEAN DISTANCE FUNCTION FOR THE PDI MODEL

INTRODUCTION

Research has demonstrated spatial density (or crowding) to be a significant stressor in animal and human populations (Galle, Grove, and McPherson, 1972; Baum and Epstein, 1975). In previous papers, the author formulated and tested a mathematical model and methodology for measuring discrete spatial density in human populations (O'Brien (1989, 1990a, 1990b)). The model, called the population density index (PDI) model, was demonstrated to provide a more accurate and flexible approach for discrete spatial density measurement than the conventional formulation. The traditional approach to measuring human physical density involves two parameters: the number of persons (n) and the geometric area (A) in which the persons dwell. The equation $D = n/A$ serves as the conceptual and computational definition for "density," "congestion," "population density," or "physical crowding," each term used interchangeably. In contrast, the PDI model is based on three parameters: n , A , and inter-object distance. The derivation of the PDI model metrics is patterned on the "square-root law" of average distances used in the physical sciences. The capability to model inter-object distance within a defined geometric plane is a significant enhancement to discrete spatial density measurement. In O'Brien (1991a), the PDI model was generalized to any finite number of density points (i.e., people).

The motivation for developing the PDI formula and model was the need to be able to measure crowding among people from variable spatial configurations such as in a typical dynamic workplace environment. The conventional density model assumes that a static description is adequate without taking into account the way in which people use an environment over time.

The PDI model has been used at the Naval Undersea Warfare Center (NUWC) Division, Newport, for density measurement (O'Brien and Kanter, 1988; Kanter and O'Brien, 1989a; 1989b) in submarine attack center concept of operations experiments (Wallin, 1987). Practical applications of the PDI model resulting from research at NUWC have been documented for a variety of disciplines in several U.S. patent applications (O'Brien, 1991c, 1991d, 1991e, 1991f).

The purpose of this report is to provide a more rigorous derivation of the PDI model than currently exists. The basis of the PDI model is the distance function in Euclidean space. All of

the measures in the model are related to distance. Thus, an attempt is made to characterize the PDI distance function in R^2 (two-dimensional Euclidean space).

DERIVATION OF THE DISTANCE FUNCTION

GENERAL CASE LATTICES

The notation and structure of this section is patterned on Morrey (1962, Chapter 8, "The Definite Integral"), where the theory of area and concept of functional uniform continuity are developed in detail. Also, the ideas of inner and outer areas of bounded sets and the idea of a planar figure developed in Morrey are germane to the present development.

In the X-Y Euclidean plane (quadrant I) of figure 1, any two consecutive abscissa (horizontal) or ordinate (vertical) points (denoted by a large dot \bullet) are assumed to be equidistant with interpoint spacing parameter δ . That is, the directed distances of the collinear point pairs $(P_1P_2) = [(x_k, y_l), (x_{k+1}, y_l)]$ and $(P_3P_4) = [(x_m, y_j), (x_m, y_{j+1})]$ are

$$\begin{aligned}\overline{P_1P_2} &= |x_{k+1} - x_k| = \delta, \\ \overline{P_3P_4} &= |y_{j+1} - y_j| = \delta,\end{aligned}\tag{1}$$

where x_k is a representative abscissa and y_j is a representative ordinate; $(x_k, y_j) > 0$. Generally, x_k, y_j will not be lattice (integer) points. In this report the units of the interpoint distance parameter δ for human populations are assumed to be feet ($\delta \geq 1$).

The interior rectangular lattice shown in figure 1 consists of n (a nonprime number) finite points arranged uniformly with R row (horizontal) and C column (vertical) points such that $n = RC$ ($n \geq 2$). The selection of an RC configuration and the computation of δ are explained in appendix A.

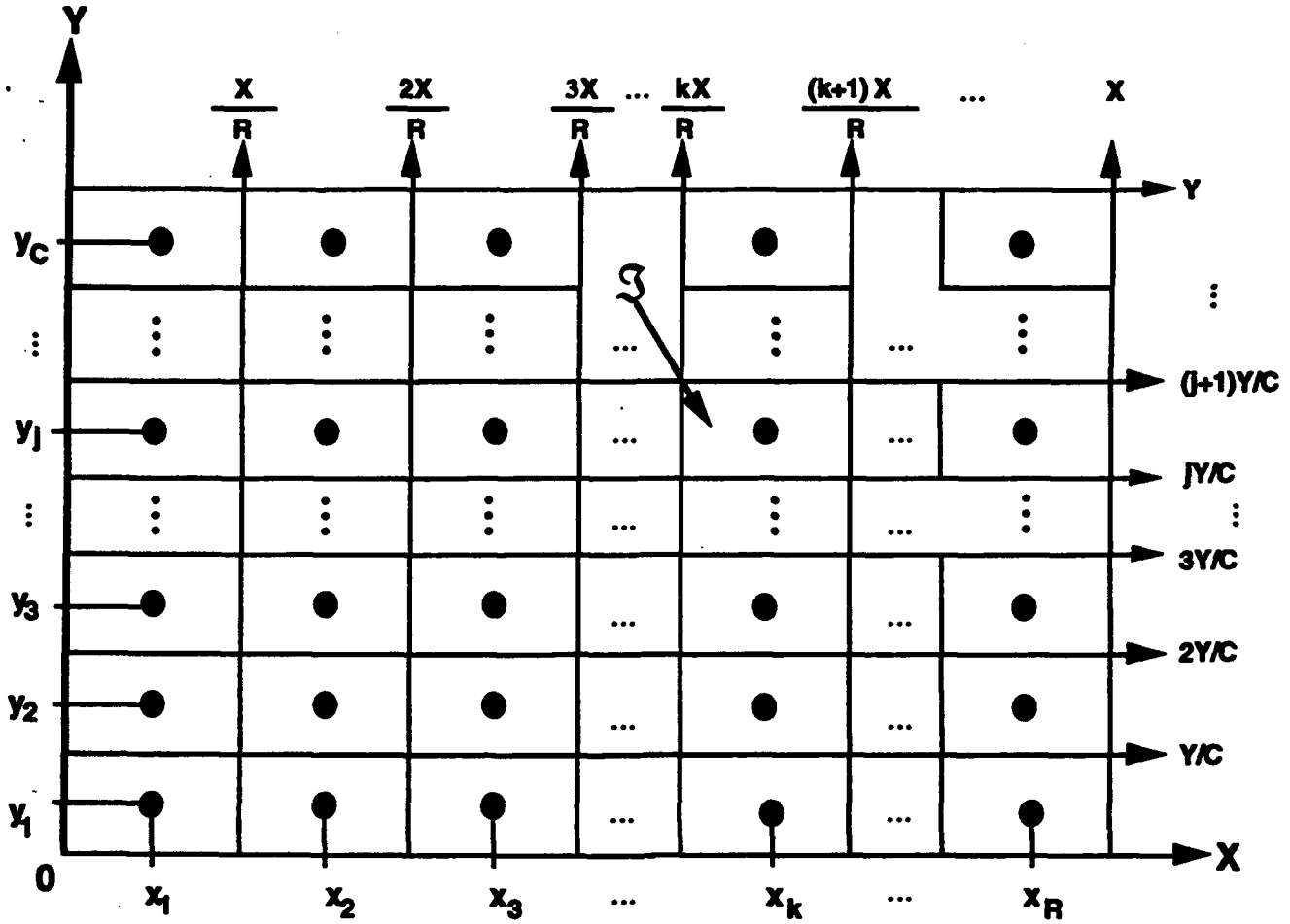


Figure 1. General Case Lattice

For a representative region 3 bounded by the nonnegative curves (see figure 1)

$$f_A(x) = (j+1)Y/C \quad (2)$$

$$g_A(x) = jY/C, \quad g_A(x) < f_A(x),$$

$$kX/R \leq x \leq (k+1)X/R, \quad 0 \leq k \leq R-1, 0 \leq j \leq C-1,$$

the area $A(3)$ is defined as

$$\begin{aligned} A(3) &= \int_{kX/R}^{(k+1)X/R} [f_A(x) - g_A(x)] dx, \\ &= XY/RC = A/n, \end{aligned} \quad (3)$$

which is seen to be a rectangle. For human populations with feet as the linear units, the restriction will be placed on the value of A/n ; viz., $A \geq n$. When $A = n$, the RC rectangular or square uniform discrete distribution is referred to as a "unit lattice"; otherwise, the homogeneous distribution of points is called a "nonunit lattice." The distinction will be understood in context. Each such rectangle will be obtained by dividing the total study area $n[A(3)]$ into $n = RC$ partitioned rectangles each, with area given by equation (3).

The connected density points in each of the horizontal and vertical intervals are defined by relations (or multiple-valued discrete constant functions):

$$\begin{aligned} f(R) = X &= (R - 1)\delta + p, \quad p > 0, \\ f(C) = Y &= (C - 1)\delta + q, \quad q > 0. \end{aligned} \tag{4}$$

Equations (4) indicate that each X or Y interval consists of two components: the length of the density points segment $[(R - 1)\delta$ or $(C - 1)\delta]$ and an excess factor (p or q). The region outside the perimeter of the uniform point arrangement [equal to $A - (R - 1)(C - 1)\delta^2$] is required to accommodate environmental objects (furniture, equipment, displays, etc.). Each of the CX intervals and RY intervals is defined by the constant functions in equations (4). The interval X will be partitioned into R subintervals, each subpartition of which will have the length shown in figure 1, and Y will be similarly divided and have the length shown in figure 1.

The derivation of the coordinate system for the general-case lattice will allow a precise graph to be drawn of any uniform rectangular distribution on a rectangular Cartesian X-Y coordinate system such that the interior RC lattice is contained within the XY exterior region. The coordinates of the density points derived from equation (4) will be generated by

$$\begin{aligned} x_k &= p/2 + (k - 1)\delta, \quad 1 \leq k \leq R, \\ y_j &= q/2 + (j - 1)\delta, \quad 1 \leq j \leq C. \end{aligned} \tag{5}$$

Then, the coordinate system for the general case will be defined as

$$\begin{aligned} (x_k, y_j) &= [(x_1, y_1), (x_2, y_1), \dots, (x_k, y_j), \dots, (x_R, y_C)] \\ &= \left[\left(\frac{p}{2}, \frac{q}{2} \right), \left(\frac{p}{2} + \delta, \frac{q}{2} \right), \dots, \left(\frac{p}{2} + (k - 1)\delta, \frac{q}{2} + (j - 1)\delta \right), \dots, \right. \\ &\quad \left. \left(\frac{p}{2} + (R - 1)\delta, \frac{q}{2} + (C - 1)\delta \right) \right]. \end{aligned} \tag{6}$$

The coordinate system of equation (6) applies to either a unit or nonunit lattice because it is derived from the general case. An example of the use of equation (6) is depicted in figure 2. The coordinates were generated from the following assumptions: $n = 6$; $R = 3$, $C = 2$ (from equation (A-4) in appendix A); $A = X \times Y = 16 \times 6$; $p/2 = 4$, $q/2 = 1$ (from (4)); $\delta = 4$ (from equation (A-5) in appendix A). Then the coordinate points are generated by $x_k = 4 + 4(k - 1)$; $y_j = 1 + 4(j - 1)$. The plot points are obtained from all $k \times j$ combinations ($k = 1, 2, 3$; $j = 1, 2$).

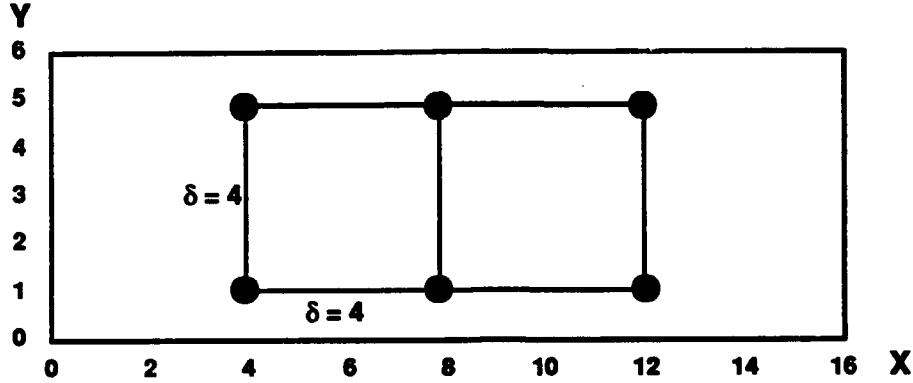


Figure 2. Example of General Case PDI Graph

SPECIAL CASE LATTICES

Each density point (\bullet) is now assumed to be the centroid (center of mass) bounded by its respective planar region (see figure 3). Let a representative region be called S . The area of S can be determined by first defining the nonnegative curves as the boundaries of S :

$$f_B(x) = (j + 1)\delta, \quad (7)$$

$$g_B(x) = j\delta, \quad g_B(x) < f_B(x),$$

$$k\delta \leq x \leq (k + 1)\delta, \quad 0 \leq k \leq R - 1, \quad 0 \leq j \leq C - 1.$$

The special case of equation (7) can be derived from equation (2) by assuming that $\delta = p = q = X/R = Y/C$ in equation (4) of the general case (i.e., proportionate commensurability between the dimensions of the outer and inner rectangular areas).

The area of S is then found by integrating between the curves $f_B(x)$ and $g_B(x)$ in the x interval, and applying the Fundamental Theorem of Calculus:

$$A(S) = \int_{k\delta}^{(k+1)\delta} [f_B(x) - g_B(x)] dx = \delta^2, \quad \delta^2 \geq 1. \quad (8)$$

This is intuitively the area of a square figure. The figure will be obtained by dividing the total area $n[A(S)]$ into $n = RC$ partitions after determining which lattice configuration will accommodate best the n points into a rectangular configuration with associated interpoint spacing parameter δ (see appendix A). Note that for commensurate (unit or nonunit) lattices, the interpoint spacing parameter is related to the region in equation (8).

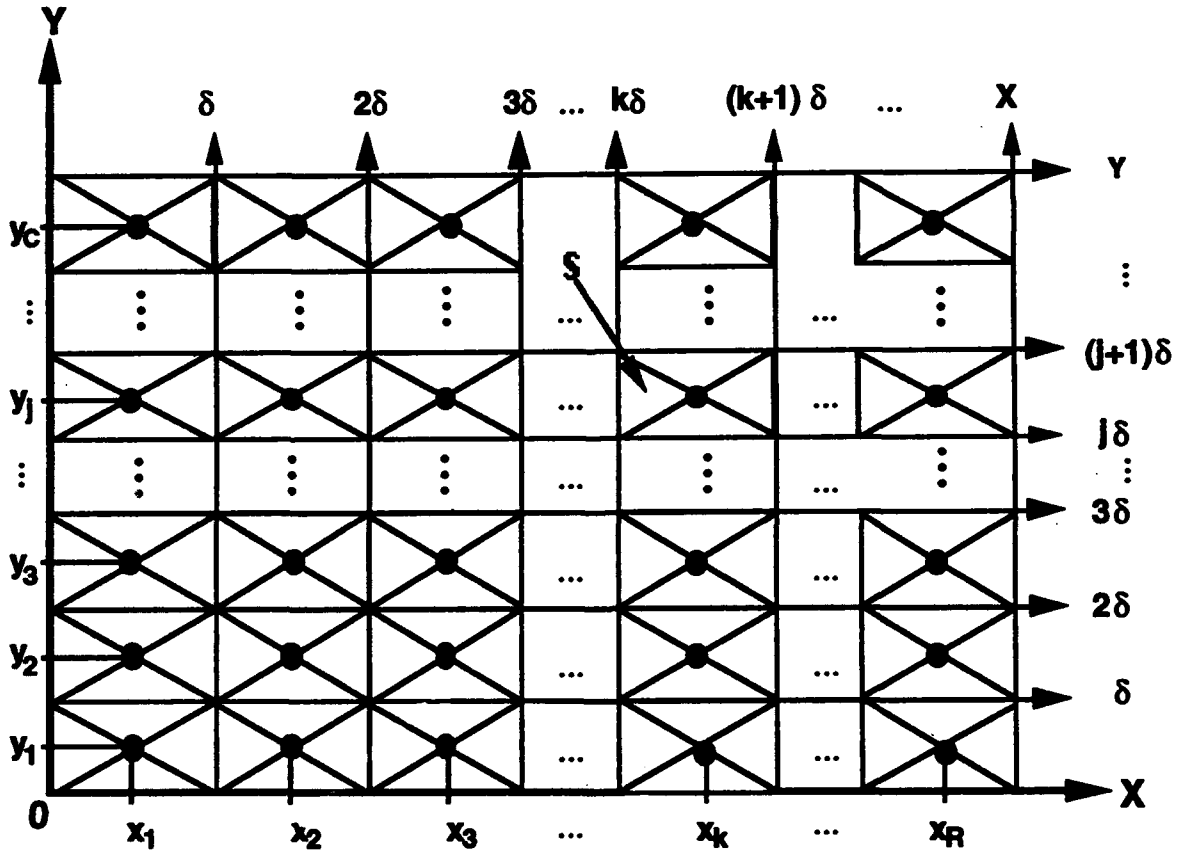


Figure 3. Special Case Lattice

Bers (1969, Vol. II, chapter 8, section 8, "Centroids of Plane Regions and Curves") gives the following definitional formulas for determining the coordinate points (x_k, y_j) of the centroid in region S:

$$(x_k, y_j): x_k = \frac{\int_{k\delta}^{(k+1)\delta} x [f_B(x) - g_B(x)] dx}{\int_{k\delta}^{(k+1)\delta} [f_B(x) - g_B(x)] dx} = \frac{\delta(2k+1)}{2},$$

$$(x_k, y_j): y_j = \frac{\int_{k\delta}^{(k+1)\delta} 1/2 [f_B(x)^2 - g_B(x)^2] dx}{\int_{k\delta}^{(k+1)\delta} [f_B(x) - g_B(x)] dx} = \frac{\delta(2j+1)}{2}.$$

Here, (x_k, y_j) represents the rule for locating all and every density point (centroid) in the entire XY area, given concisely as

$$(x_k, y_j) = \left[\left(\frac{\delta}{2} + (k-1)\delta \right), \left(\frac{\delta}{2} + (j-1)\delta \right) \right]$$

$$= [(x_1, y_1), (x_2, y_1), (x_3, y_1), \dots, (x_k, y_1),$$

$$(x_1, y_2), \dots, (x_k, y_2), \dots, (x_k, y_j), \dots, (x_R, y_C)]$$

$$= \left[\left[\frac{\delta}{2}, \frac{\delta}{2} \right], \left[\frac{3\delta}{2}, \frac{\delta}{2} \right], \left[\frac{5\delta}{2}, \frac{\delta}{2} \right], \dots, \left[\frac{\delta(2R-1)}{2}, \frac{\delta}{2} \right], \right.$$

$$\left. \left[\frac{\delta}{2}, \frac{3\delta}{2} \right], \dots, \left[\frac{\delta(2R-1)}{2}, \frac{3\delta}{2} \right], \dots, \right.$$

$$\left. \left[\frac{\delta}{2} + (k-1)\delta, \frac{\delta}{2} + (j-1)\delta \right], \dots, \left[\frac{\delta(2R-1)}{2}, \frac{\delta(2C-1)}{2} \right] \right\},$$

$$1 \leq k \leq R, \quad 1 \leq j \leq C.$$

The coordinate system of equation (10) applies to unit lattices and commensurate nonunit lattices. Figure 4 is an example of equation (10) applied to a 3 x 2 unit lattice ($\delta = 1$ from equation (A-5) in appendix A). Note that $X/R = Y/C = p = q = \delta = \sqrt{XY/RC} = 1$ because all unit lattices are commensurate. The graph is plotted from equation (10) by $x_k = k - 0.5$; $y_j = j - 0.5$ ($k = 1, 2, 3$; $j = 1, 2$).

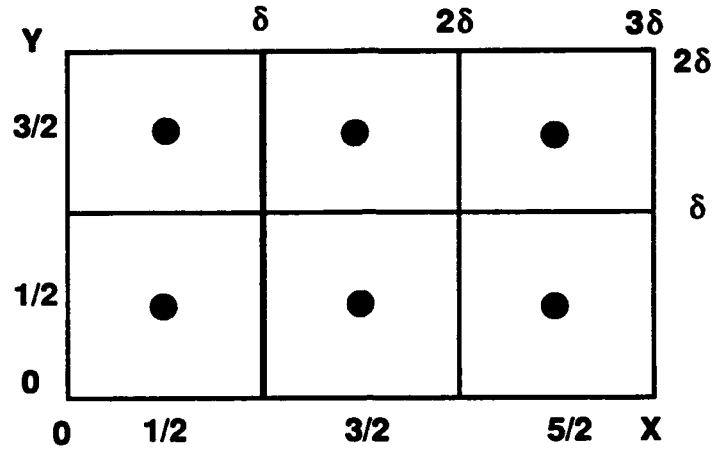


Figure 4. Example of Special Case PDI Graph (Unit Lattice)

Figure 5 is an example of a graph for a nonunit commensurate lattice with $n = 15$ points within area of 40 ft x 24 ft. Note that $X/R = Y/C = p = q = \delta = \sqrt{XY/RC} = 8$. Plot points are generated from equation (10): $x_k = 4 + 8(k - 1)$; $y_j = 4 + 8(j - 1)$.

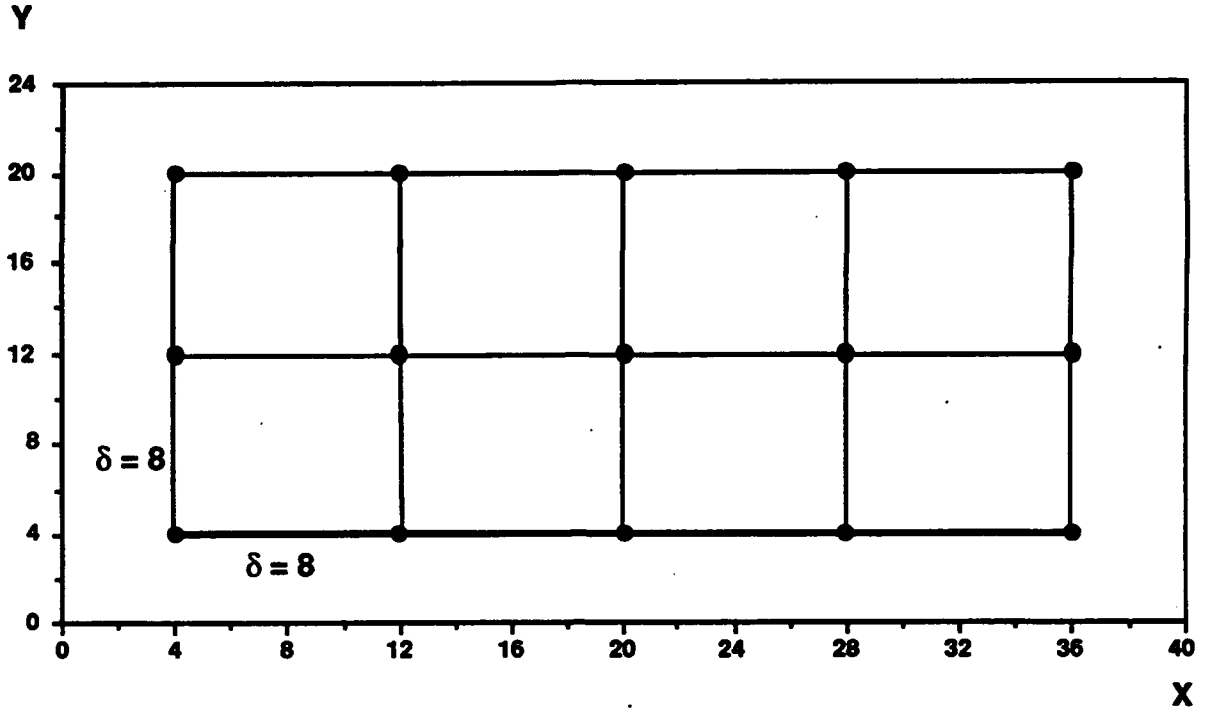


Figure 5. Example of Special Case PDI Graph (Commensurate Nonunit Lattice)

GENERALIZED DISTANCE FUNCTION IN A LATTICE

Since the coordinate points in the PDI lattice can now be specified completely, the PDI “exact” and “approximate” distance formulas can be derived (O’Brien, 1990b, 1991b). Here is derived the generalized, Euclidean distance formula for any PDI lattice (nonunit lattice and thereby the unit lattice as a special case) and any nonuniform distribution. First shown is the derivation for a lattice using the general case notation system. The derivation applies equally to the special case by assuming commensurability.

Let any density point in the X-Y plane be called (x_k, y_j) and let a second distinct point be called (x_{k+i}, y_{j+l}) . Then, from equation (6),

$$(x_k, y_j) = (p/2 + (k - 1)\delta, q/2 + (j - 1)\delta), \quad (11)$$

$$(x_{k+i}, y_{j+l}) = (p/2 + (k + i - 1)\delta, q/2 + (j + l - 1)\delta),$$

$$1 \leq k \leq R - 1, \quad 1 \leq j \leq C - 1,$$

$$2 \leq k+i \leq R, \quad 2 \leq j+l \leq C.$$

Bers (1969, Vol. I) shows that the classical Pythagorean distance formula for any two points in a Cartesian plane can generally be derived from the integral calculus arc length formula, given for our notation as

$$\mathcal{L} = \int_{x_k}^{x_{k+i}} \sqrt{1 + [f'(x)]^2} dx. \quad (12)$$

The quantity $f'(x)$ is the first derivative of the function $f(x)$, taken to be a generalized single-valued relation for two points in a Euclidean X-Y plane specified by the first degree equation $f(x) = a + bx$, for the slope intercept a and linear slope b .

Since $f'(x) = \frac{d[f(x)]}{dx} = D_x(a + bx) = b$, the constant slope of the points in equation (11) can be defined as $b = \frac{y_{j+l} - y_j}{x_{k+i} - x_k} = \frac{\delta l}{\delta i}$. Then,

$$\begin{aligned} \mathcal{L} &= \int_{x_k}^{x_{k+i}} \sqrt{1 + \left(\frac{l}{i}\right)^2} dx, \\ &= \delta \sqrt{i^2 + l^2}, \end{aligned} \quad (13)$$

which is seen to be of the form for the standard bivariate Pythagorean theorem scaled by a constant:

$$\mathcal{L} = \delta \sqrt{(x_{k+i} - x_k)^2 + (y_{j+l} - y_j)^2}. \quad (14)$$

Bers (1969, Vol. I, p. 279) terms equation (12) the "length formula." It may also be viewed as an average -- the average length of one pair of points. The length (distance) between any one pair of points in the uniform RC lattice can be generalized to an average among all possible pairs of RC points since each point pair defines a simple linear function each of which possesses a piecewise continuous first derivative. The average pair-to-pair distance, summed over all pairs of points, will be the average of all the line-to-line curves (total length), since the connected graph defines a multiple-valued relation (Bers, 1969, Vol. I, page 279). That is, the uniform average distance in the total lattice is

$$\bar{d} = \frac{\sum_{k=j=1}^n L_{kj}}{C(n,2)}, \quad (15)$$

where

$$C(n,2) = \frac{(RC)!}{2!(RC-2)!} = \frac{n(n-1)}{2}, \quad (n \geq 2), \quad (16)$$

is the combinatorial expression specifying the total number of nonredundant pairwise-connected lines from n nodes and the exact summation index limits are given in equation (11). The uniform lattice distance equation (15) can be further expressed in a more computational convenient form as

$$\bar{d} = \delta \bar{\Delta}, \quad (17)$$

where δ is given in appendix A and $\bar{\Delta}$ is the unit lattice average distance, which has been derived in O'Brien (1991a) as

$$\bar{\Delta} = \frac{12 \sum_{i=1}^{R-1} \sum_{j=1}^{C-1} (R-i)(C-j) \sqrt{i^2 + j^2} + RC(R^2 + C^2 - 2)}{3(RC)(RC-1)}, \quad (18)$$

where R is the number of horizontal points in each row of the unit lattice, C is the number of vertical points in each column of the unit lattice, and RC is the total number of density points in the unit lattice.

An accurate approximation to equation (18) exists when n is not small. This relation is derived under the assumption that there is a continuous uniform distribution within a rectangular plane. The objective is to find the average distance between any two randomly selected points of a convex set. The approximation formula* (Santalo, 1976, formula 4.18, page 49) is as follows:

$$\bar{\Delta}' = \frac{1}{15} \left[\frac{R^3}{C^2} + \frac{C^3}{R^2} + d \left(3 - \frac{R^2}{C^2} - \frac{C^2}{R^2} \right) + \frac{5}{2} \left[\frac{C^2}{R} \ln \left(\frac{R+d}{C} \right) + \frac{R^2}{C} \ln \left(\frac{C+d}{R} \right) \right] \right], \quad (19)$$

* The author gratefully acknowledges an anonymous referee of *The American Mathematical Monthly* for suggesting equation (19) (in correspondence related to O'Brien, 1990c).

where $d = \sqrt{R^2 + C^2}$ and \ln is the natural logarithm operator.

Calculations have shown equation (19) to be a good approximation to equation (18). For example, for n under 100, the maximum discrepancy is less than 10 percent. Equation (19) is an interesting example where a continuous distribution relation is applied to a discrete distribution to obtain an approximation to the latter. In the limiting case, as RC approaches infinity, the difference between equations (18) and (19) approaches zero.

In conclusion, for any finite, discrete, uniform distribution with distance between any two points δ , the generalized average Euclidean distance in any PDI lattice among all possible pairs of RC points will be $\bar{d} = \delta \bar{\Delta}$ or $\delta \bar{\Delta}' \approx \bar{d}$. If a unit lattice ($\delta = 1$), then $\bar{d} = \bar{\Delta}$ or $\bar{\Delta}' \approx \bar{d}$. Selected values of $\bar{\Delta}$ calculated from equation (18) are given in appendix B for all RC configurations from $R \times C = 2 \times 2$ to $R \times C = 100 \times 100$ ($n = 10,000$ density points).

GENERALIZED DISTANCE FUNCTION IN A NONLATTICE

Here, density points can fall anywhere within the X - Y geometric area, subject to restrictions specified earlier. The average Euclidean distance is calculated by equation (15) from known coordinate points as

$$\bar{d} = \frac{\sum_{i < j} \sqrt{(x_i - x_j)^2 + (y_i - y_j)^2}}{C(n,2)}, \quad (20)$$

where (x_i, y_i) , (x_j, y_j) ($i = 1, 2, \dots, n$; $j = 1, 2, \dots, n$) denote the coordinate locations for the density points ($n > 1$) within the rectangular study area $X \times Y$ with arbitrary origin O . Equation (20) is the form used for calculating the population density measure of observed density points (i.e., PDI_{act} , defined below in equation (29)).

An approximation to equation (20) is useful because exact (x_i, y_i) , (x_j, y_j) coordinates cannot always be obtained. Recently, O'Brien (1991b) derived an approximation PDI method by assuming knowledge of the relative location of the density objects when (x_i, y_i) , (x_j, y_j) data were unavailable.

If one assumes that the study area $A = X \times Y$ has been partitioned into $n = RC$ rectangles, each with subarea given by equation (3), then the following abbreviated calculation routines can be derived.

Define a cell density measure,

$$D_{jk} = n_{jk} / A_{jk}, \quad (21)$$

where n_{jk} is the number of objects observed to be within each of the subareas $A_{jk} = A/n$ ($j = 1, 2, \dots, R; k = 1, 2, \dots, C$), $0 \leq n_{jk} \leq A_{jk}$, $0 \leq D_{jk} \leq 1$. Then, define a cell indicator variable I :

$$I_{jk} = \begin{cases} 1 & \text{if } D_{jk} \neq 0, \\ 0 & \text{if } D_{jk} = 0. \end{cases} \quad (22)$$

Let

$$m = \sum_{k=1}^R \sum_{j=1}^C I_{jk}, \quad nD \leq m \leq n, \quad (23)$$

where $D = n/A$ is obtained from equation (21) as an average cell density with weights spread over all cells; i.e., $D = \sum_{k=1}^R \sum_{j=1}^C D_{jk} n^{-1}$. The measure m represents the total number of RC partitions occupied by at least one object. In practice, n_{jk} is taken as the smallest integer value. Likewise, m is taken to be the largest integer value.

Hence, equation (17) can be redefined to give the following approximation to equation (20):

$$\bar{d}' = \delta'_{\text{eff}} \bar{\Delta}, \quad (24)$$

where

$$\delta'_{\text{eff}} = \left(\frac{\sum_{k=1}^R \sum_{j=1}^C D_{jk}}{m} \right)^{-1/2} = \left(\frac{mA_{jk}}{n} \right)^{1/2}, \quad 1 \leq \delta'_{\text{eff}} \leq D^{-1/2}. \quad (25)$$

δ'_{eff} is obtained from equation (21) as an average cell density with weights spread over only the m occupied cells. The limits of equation (24) follow immediately by substituting the lower and upper limits of m given in equation (23); viz., $\bar{\Delta} \leq \bar{d}' \leq \bar{\Delta} \sqrt{A/n}$. Noting that $1 \leq \delta \leq \sqrt{A/n}$ (see appendix A) and assuming, in practice, that $1 \leq \delta'_{\text{eff}} \leq \delta$, it then follows that

$$\bar{d}_{\text{max}} \leq \bar{d}' \leq \bar{d}_{\text{min}}, \quad (26)$$

where \bar{d}_{\min} and \bar{d}_{\max} are, respectively, the lower and upper distance measures in the exact PDI model (O'Brien, 1990b). The relationship of (26) translates directly into a proof of the bounds of the approximate PDI measure ($PDI'_{act} = \sqrt{D/\bar{d}} = [D\sqrt{n/m}]/\bar{\Delta}$; i.e., PDI'_{act}) is bounded by the PDI_{\min} and PDI_{\max} relations defined in O'Brien (1990b) and in equations (27) and (28) below.

ALTERNATIVE DISTANCE MODELS

Thus far, the distance function has been derived for a rectangular configuration of points by assuming a rectangular exterior region. Mathematically, there is good reason for doing this because a square or rectangle can be drawn around any closed curve (Steinhaus, 1969).

Occasionally, the environment of interest may be modeled by curved configurations such as ellipses or circles, the latter being the easier to work with. Circular distributions have two advantages. First, for regions nearly square, a circle offers a more compact concentration of points, which may provide more realistic bounds on the density measure for highly cluttered environments. Second, any number n of points (including prime numbers) can be placed uniformly on a circle of radius r with linear point-to-point distance $d = 2r \sin(180/n)$. Based on this chord length measure, the author recently constructed a PDI model for discrete spatial density for circular distributions (O'Brien, 1992).

SELECTED PROOFS

PROOF THAT $PDI_{\min} \leq PDI_{\text{act}} \leq PDI_{\max}$

First, a statement of the relationships involved in this proof is given as follows:

$$\text{Lower bound: } PDI_{\min} = \frac{1}{\delta \bar{\Delta}} \sqrt{\frac{n}{A}}, \quad (27)$$

$$\text{Upper bound: } PDI_{\max} = \frac{1}{\bar{\Delta}} \sqrt{\frac{n}{A}}, \quad (28)$$

$$\text{Actual PDI: } PDI_{\text{act}} = \frac{1}{\bar{d}_{\text{act}}} \sqrt{\frac{n}{A}}. \quad (29)$$

The terms n , A , $\bar{\Delta}$, and \bar{d}_{act} (equivalent to equation (20)) are used here as defined in this report; δ is defined in appendix A.

Now, to the proof. From the relationships of equations (27), (28), and (29), a formal statement of the relationship to be proven is as follows:

$$\frac{1}{\delta \bar{\Delta}} \sqrt{\frac{n}{A}} \leq \frac{1}{\bar{d}_{\text{act}}} \sqrt{\frac{n}{A}} \leq \frac{1}{\bar{\Delta}} \sqrt{\frac{n}{A}}. \quad (30)$$

To prove that equation (30) is a true statement, three assumptions are required:

$$\bar{d}_{\text{act}}, \delta, \text{ and } \bar{\Delta} \text{ are measured in linear units of feet,} \quad (31)$$

$$\delta \geq 1, \quad (32)$$

$$\bar{d}_{\text{act}} \leq \delta \bar{\Delta}. \quad (33)$$

The first assumption (31) is self-explanatory. The second assumption (32) is deemed reasonable because it amounts to saying that if persons are positioned uniformly the head-to-head distance (δ) is about 1 foot. Although (32) would not be a reasonable assumption for areal units of, say, square miles, (32) is reasonable when the areal units are square feet. (See O'Brien, 1991f, for the finite "macro" PDI model when areal units are square miles.)

The third assumption (33) states that, for a given geometric area to be studied in a density analysis, the actual clustering of the density points (i.e., people) in that area (with associated density \bar{d}_{act}) will not be greater than the maximum theoretical dispersion provided by the

relation $\delta\bar{\Delta}$ (equation (17)). The region outside $\delta\bar{\Delta}$ is assumed to contain physical objects such as furniture, equipment, etc., making it unlikely that density points will be observed in that region. Empirical evidence from Monte Carlo simulations in O'Brien (1989) is cited in support of (33). In effect, (33) assumes that the persons are maximally dispersed in accord with the relation $\delta\bar{\Delta}$. Figure 6 describes the essential meaning of (33).

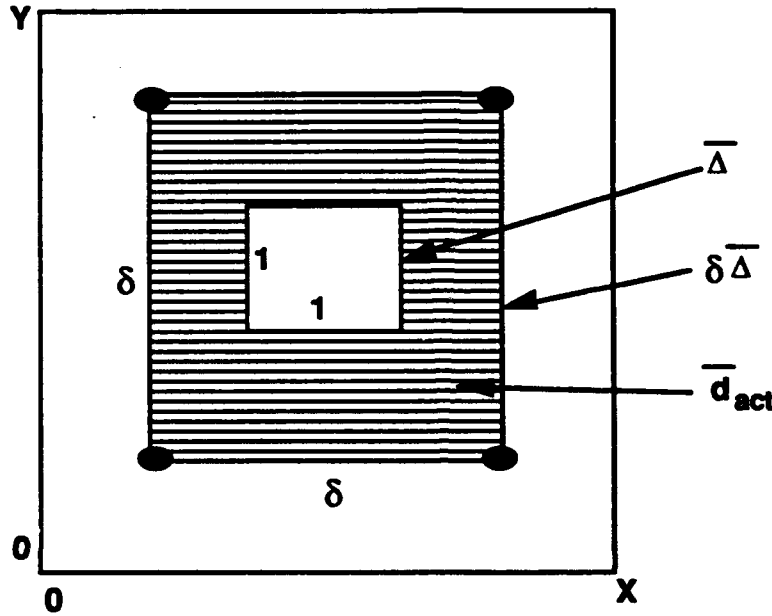


Figure 6. Intuitive Justification for Third Assumption

The formal proof of equation (30) can now be given in detail. The proof is presented in three parts. The first part states

$$\frac{1}{\delta\bar{\Delta}} \sqrt{\frac{n}{A}} \leq \frac{1}{\bar{d}_{act}} \sqrt{\frac{n}{A}}. \quad (34)$$

Simplifying and rearranging the terms of equation (34) gives the following relationship:

$$\bar{d}_{act} \leq \delta\bar{\Delta}, \quad (35)$$

which follows directly from (33).

The second part of the proof states that

$$\frac{1}{\bar{d}_{act}} \sqrt{\frac{n}{A}} \leq \frac{1}{\bar{\Delta}} \sqrt{\frac{n}{A}}. \quad (36)$$

Simplifying and rearranging the terms of equation (36) gives the following relationship:

$$\bar{\Delta} \leq \bar{d}_{act}. \quad (37)$$

From (33) the following relationship can be established:

$$\frac{\bar{d}_{act}}{\bar{\Delta}} \leq \delta, \quad (38)$$

from which it can be deduced that

$$\frac{\bar{\Delta}}{\bar{d}_{act}} \leq \frac{1}{\delta}. \quad (39)$$

Since, by (32), it follows that $1/\delta \leq 1$, then it can be deduced that $\bar{\Delta}/\bar{d}_{act} \leq 1$, from which it follows that $\bar{\Delta} \leq \bar{d}_{act}$.

The third part of the proof asserts that

$$\frac{1}{\delta \bar{\Delta}} \sqrt{\frac{n}{A}} \leq \frac{1}{\bar{\Delta}} \sqrt{\frac{n}{A}}. \quad (40)$$

The relationship between the lower and upper limits of equation (40) follows necessarily from the proofs given for equations (34) and (36) by the transitivity property of relations. It can be readily seen that equation (40) reduces algebraically to $\delta \geq 1$, which follows directly from (32). Thus, the statement of equation (30) has been shown to be true as derived from the stated definitions and assumptions.

The proof that the approximate PDI formula is bounded by the minimum and maximum bounds given in equations (27) and (28) follows from equation (26) and from the definition of the approximate PDI measure.

PROOFS FOR δ_{eff}

From O'Brien (1990b, equation(9)), δ_{eff} is defined as

$$\delta_{\text{eff}} = \frac{\bar{d}_{\text{act}}}{\bar{\Delta}}. \quad (41)$$

The objective is to show that $\delta_{\text{eff}} \geq 1$. Since $\frac{\bar{d}_{\text{act}}}{\bar{\Delta}} \geq 1$, as proven from equation (36), equation (41) follows.

The proof that $\delta/\delta_{\text{eff}} \geq 1$ is as follows:

By definition, $\delta_{\text{eff}} = \frac{\bar{d}_{\text{act}}}{\bar{\Delta}}$; then, $\delta/\delta_{\text{eff}} = \frac{\delta\bar{\Delta}}{\bar{d}_{\text{act}}} \geq 1$, which follows because it reduces to $\delta\bar{\Delta} \geq \bar{d}_{\text{act}}$, which was established previously in (33).

Because the quantity δ_{eff} is a "pure number" (i.e., it has no dimensions because they cancel out as in the above definition), it provides a pure measure of relative change in population density.

The reader may also note that in the approximation model $\delta'_{\text{eff}} \geq 1$ and $\delta/\delta'_{\text{eff}} \geq 1$ follows from the derived limits given in equation (25) and the relationship given in equation (26).

SUMMARY

This report has presented derivations of various distance functions that relate to the author's three-parameter square-root model for measuring discrete spatial density in finite populations. The model, called the Population Density Index (PDI) model, was developed to capture dynamic density relations among persons within a naturalistic environment. An "exact" model and an "approximate" model were presented.

The derivations related a generalized Euclidean distance function to the fundamental measures in the model (PDI_{act} , the approximation measure PDI'_{act} , their lower and upper bounds, and the density rate indices δ_{eff} and δ'_{eff}). Coordinate systems were derived for plotting graphs of the PDI lattices and calculating the distance measures.

Also derived was the algorithm required to select a conformal lattice and the average uniform distance among the lattice points based on the number of density points to be analyzed within the reference quadrilateral area.

Average Euclidean distance values ($\bar{\Delta}$) were presented for unit lattices up to a 100 x 100 matrix. Using these values, researchers will be able to compute lower and upper bounds of the PDI measures for up to 10,000 density objects.

APPENDIX A SELECTING A UNIT LATTICE AND INTERPOINT DISTANCE PARAMETER

DERIVATION OF THE ALGORITHM

In this appendix, the algorithm is presented for (1) determining a unique finite, discrete, conformal RC lattice and (2) computing the average interpoint distance among the RC points.

To begin, it is assumed that n (sample size) and $A = X \times Y$ (the outer rectangular geometric area) are known. If n is a prime number (like 5 or 13 or 29), augment n by 1 before determining the rectangular/square dimensions of the unit lattice. The derivation of the algorithm for selecting an RC lattice is developed from concepts of number theory (Ore, 1967). In particular, interest is centered on sets and subsets of composite numbers that can be expressed as rectangular or square integers; i.e., positive (nonprime) integers that are two-integer products.

The value of n can be expressed in terms of the prime factors of the whole number:

$$n = \prod_{j=1}^r P_j^{\alpha_j}, \quad (A-1)$$

where P_j represents the j th prime number and α_j is the number of occurrences of the j th prime number of n . For example, composite 60 can be decomposed into $P_1^{\alpha_1} P_2^{\alpha_2} P_3^{\alpha_3} = 2^2 \times 3 \times 5$. Next, it is desired to derive the total number of possible RC ($n = R \times C$) product configurations of n in order to create the set of RC configurations; the latter will be a subset of the former. This number can be derived as follows.

Let $\tau(n)$ represent the number of all possible configurations of a composite integer n . Then it can be shown that this quantity is obtained from equation (A-1) by

$$\tau(n) = \prod_{j=1}^r (\alpha_j + 1). \quad (A-2)$$

For example, 60 can be partitioned into $(2+1)(1+1)^2 = 12$ two-integer products.

Next, the set of the $\tau(n)$ configurations is examined to select only those nontrivial and/or nonredundant configurations. Let $\Phi(RC)$ represent the total number of nonredundant and nontrivial $R \times C$ configurations for composite n , $\tau(n) \supset \Phi(RC)$. The trivial configurations are those for which $n = n \times 1$ or $1 \times n$, and the redundant configurations are the multiplicative, commutative equivalents of $R \times C$; i.e., $R \times C = C \times R$ ($R \geq C$) (e.g., $10 \times 4 = 4 \times 10$). Then,

$$\Phi(RC) = \frac{\tau(n) - 2 + S}{2}, \quad (A-3)$$

where $S = 0$ when n is a rectangular number, and $S = 1$ when n is a square number.* The set of all such specified configurations is denoted P of size $\Phi(RC) = m$; $P = \{R_1C_1, R_2C_2, \dots, R_iC_i, \dots, R_mC_m\}$, $(R_i \geq C_i)$. For example, if $n = 60$, then $\Phi(RC) = [(3 \times 2 \times 2) - 2 + 0]/2 = 5$; $P = \{30 \times 2, 20 \times 3, 15 \times 4, 12 \times 5, 10 \times 6\}$. Note that the trivial $(60 \times 1, 1 \times 60)$ and redundant commutative equivalent configurations $(2 \times 30, 3 \times 20, 4 \times 15, 5 \times 12, 6 \times 10)$ have been eliminated from P . Likewise, for $n = 100$, $\Phi(100) = \Phi(2^2 \times 5^2) = [(3 \times 3) - 2 + 1]/2 = 4$; $P = \{50 \times 2, 25 \times 4, 20 \times 5, 10 \times 10\}$.

Selection of a unique RC lattice with interpoint distance parameter δ is accomplished by the following guidelines.

Select the $R \times C$ lattice configuration (usually one) with dimensions most commensurate with the exterior $X \times Y$ dimensions; i.e., the one for which $X/Y - R/C$ is a minimum absolute difference ($X \geq Y, R \geq C$). Determine the uniform interpoint spacing parameter $\delta = \sqrt{A/n} = \sqrt{XY/RC}$ as defined in O'Brien (1990b, equation (3)). Next, test for conformity of the dimensions of the selected lattice to the study area dimensions by the quantities $(R - 1)\delta$ and $(C - 1)\delta$. If either of the R, C dimensions is nonconformal (i.e., $(R - 1)\delta \geq X$ or $(C - 1)\delta \geq Y$), then conform the lattice dimensions by adjusting δ by the relation $\delta = \min[X/(R - 1), Y/(C - 1)] - 0.1$. Finally, in the rarest of instances, when commensurability is achieved simultaneously by more than one lattice configuration, the researcher should approximate δ as above for each configuration, and then the $R \times C$ configuration will be that associated with the maximum δ value. If plural maxima δ occur, select the $R \times C$ configuration associated with the smallest value of $\bar{\Delta}$, given in appendix B.

The symbolic specification of the above guidelines can be stated as follows. Because the desired discrete $R \times C$ lattice must be unique, the selection mechanism requires a complex

* Equation (A-3) is not proven nor could a proof be found in the mathematical literature. Its correctness seems intuitively obvious. For example, for a number to be square, it is necessary and sufficient that all exponents in the prime factorization (equation (A-1)) be even (Ore, p. 42), which implies that $\tau(n)$ is odd, as is $\tau(n) - 2$, but adding 1 (S) makes $\Phi(RC)$ even. Finally, dividing by 2 eliminates the rectangular duplicates in $\tau(n) + S - 2$. The same logic applies to rectangular numbers, thus completing the proof outline.

two-step procedure. First, the following commensurability relation is determined from the dimensions of A and each element of the set P:

$$R_k C_k = \min_{1 \leq i \leq m} \left| \left[\frac{\max(X, Y)}{\min(X, Y)} - \frac{\max(R_i, C_i)}{\min(R_i, C_i)} \right] \right| \quad (1 \leq k \leq m). \quad (\text{A-4})$$

Then, based on equation (A-4) above and equation (4) in the main body of the text, δ is determined from one of the following four mutually exclusive and exhaustive conditions:

$$\delta = \begin{cases} \sqrt{\frac{\bar{\Delta}}{n}} & \text{if } k = 1 \text{ and } p > 0 \text{ and } q > 0 \quad (\text{A-5}) \\ \min \left[\left(\frac{X}{R-1}, \frac{Y}{C-1} \right) - 0.1 \right] & \text{if } k = 1 \text{ and } p \leq 0 \text{ or } q \leq 0 \quad (\text{A-6}) \\ \max_{1 \leq l \leq k} \left\{ \min_{2 \leq k \leq m} \left[\left(\frac{X}{R_k-1}, \frac{Y}{C_k-1} \right) - 0.1 \right] \right\} & \text{if } k > 1 \text{ and } l = 1 \quad (\text{A-7}) \\ \min_{2 \leq l \leq k} [\bar{\Delta}(R_l, C_l)] & \text{if } k > 1 \text{ and } l > 1 \quad (\text{A-8}) \end{cases}$$

where p, q are defined in equation (4). In (A-5) through (A-8), $\delta \geq 1$ by definition. Also, it may be proven that $\delta \leq \sqrt{\bar{\Delta}/n}$ based on equation (4) where it can be deduced that $(R-1)\delta < X$, $(C-1)\delta < Y$, and for commensurate lattices ($\delta \leq \sqrt{\bar{\Delta}/n}$), $\delta = X/R = Y/C$. This relationship places an upper bound on δ that is important in the proofs and derivations of the text.

Figure A-1 summarizes the algorithm for the RC lattice selection and computation of δ . In summary, if $k = 1$, $R_k C_k$ is the lattice selected from equation (A-4) and δ is selected from equation (A-5) or equation (A-6). If $k > 1$, δ is selected from equation (A-7) and R & C is selected as the lattice associated with the maximum δ in equation (A-7). Finally, if (A-7) provides a plurality of δ values, then (A-8) is used, which selects the R_l, C_l ($2 \leq l \leq k$) lattice associated with the smallest $\bar{\Delta}$ value. Appendix B contains the required $\bar{\Delta}$ values computed to five decimal places. Note that for a unit lattice, or commensurate nonunit lattice, $k = 1$ and equation (A-5) computes the correct δ . Hansen et al. (1953, Vol. I) provides an interesting discussion of commensurate nonunit lattices related to a square-root law for distances in the field of discrete finite-population sampling theory when equation (A-5) applies.

Thus, equations (A-4) through (A-8) provide a unique, conforming lattice with associated interpoint distance parameter δ . A table of prime numbers and factorizations of composite numbers is an indispensable tool for implementing equation (A-4). See Lehmer (1941, 1961) for extensive tables and Abramowitz and Stegun (1964) for abbreviated tables.

These calculations assure that the lengths of the R and C line segments of the nonunit lattice, $(R - 1)\delta$ and $(C - 1)\delta$, containing human density points do not exceed the dimensions of the study area. The utility of adjusting δ (when so required) as recommended resides in plotting minimum/maximum dispersions of the RC density points in the study area as given in equations (6) and (10).

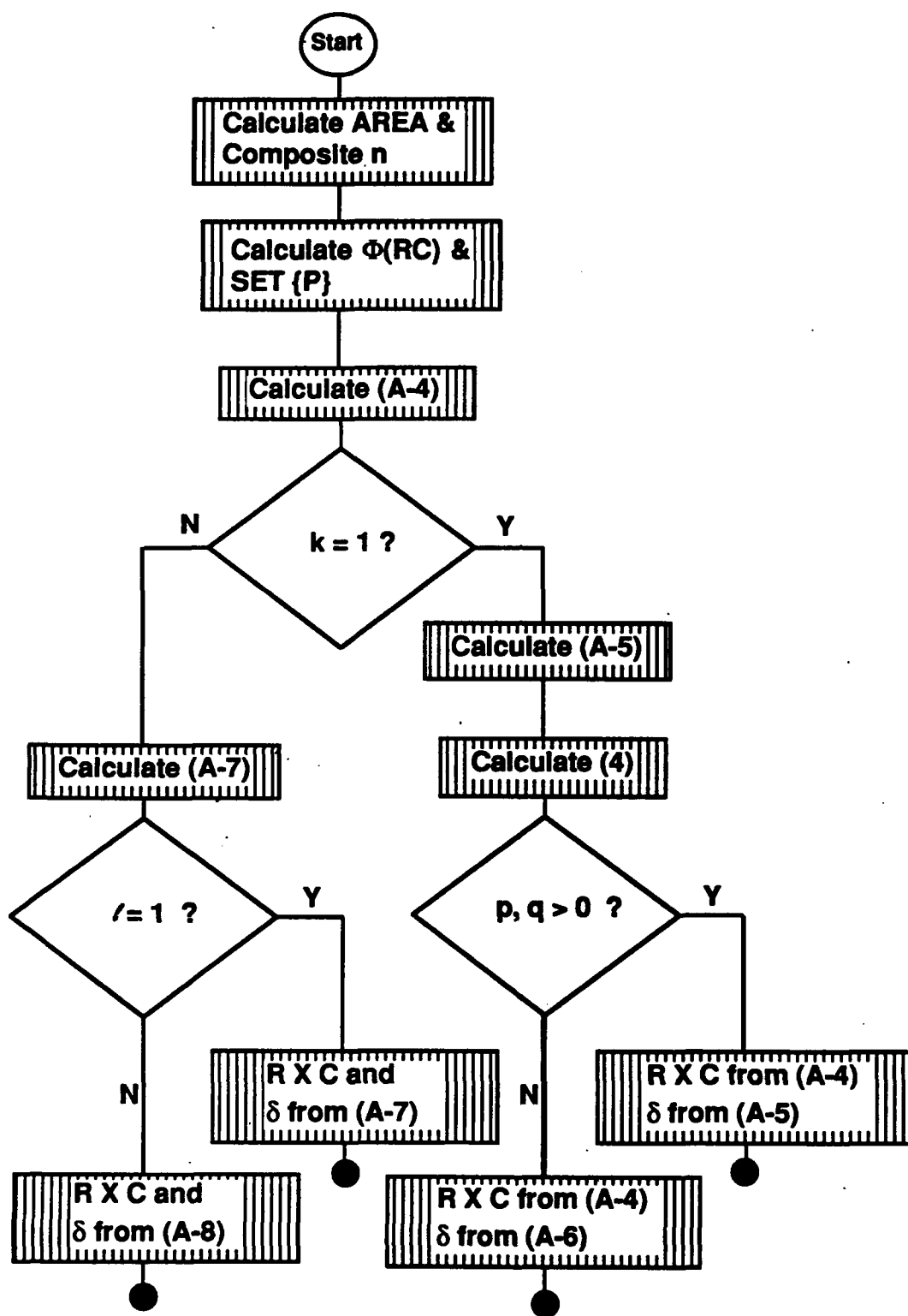


Figure A-1. Flowchart for Determining R H C Unit Lattice and Interpoint Distance Parameter δ

NUMERICAL EXAMPLES

Three artificial examples are selected to demonstrate the procedures. A complete setup is provided. The flowchart in figure A-1 is useful in tracing the decision logic.

In the first example, the data are as follows: $n = 12$, $A = 25 \times 25 \text{ ft}^2$. It is obvious that $n = 12$ provides two nontrivial, nonredundant choices ($\Phi(12) = 2$); viz., $R_1C_1 = 6 \times 2$ or $R_2C_2 = 4 \times 3$. Because $X/Y = 1$, $R_2C_2 = 4 \times 3$ comes closest to satisfying equation (A-4). Because $k = 1$, first compute $\delta = 7.22$ (from equation (A-5)); R, C is found to be conformal (each row/column "fits" inside the outside 25 ft^2 area in accord with equation (4)). Thus, $R = 4$, $C = 3$, and $\delta = 7.22$.

In the second example, $n = 64$ and $A = 50 \times 5 \text{ ft}^2$. This example is one of those rare possibilities. For $n = 64$, $\tau(64) = 7$; $\Phi(RC) = [7 + 1 - 2]/2 = 3$, and $P = \{32 \times 2, 16 \times 4, 8 \times 8\}$. Applying equation (A-4) shows that 32×2 and 16×4 are equally commensurate ($k > 1$); i.e., $|10 - 16| = |10 - 4|$. Thus, because $k = 2$ and l is undetermined, apply equation (A-7), giving $\delta = \max \{1.57, 1.51\} = 1.57 (l = 1)$. The configuration associated with the largest δ value is 16×4 . Thus, $R = 16$, $C = 4$, and $\delta = 1.57$ for this data distribution.

As an example requiring equation (A-8) for determining $R \times C$ and δ , consider the data: $A = 80 \times 16 \text{ ft}^2$, $n = 32$, $P = \{16 \times 2, 8 \times 4\}$. Here, applying (A-4) to the above data distributions produces $|5 - 8| = |5 - 2|$ (i.e., $k = 2$), and (A-7) produces $\delta = \max \{(5.23, 5.23)\} (l > 1)$, which is clearly ambiguous. But $\min [\bar{\Delta}(16 \times 2), \bar{\Delta}(8 \times 4)] = \min (5.59, 3.27) = \bar{\Delta}(8 \times 4)$. Thus, $R \times C = 8 \times 4$, and $\delta = 5.23$.

In general, the reader will note that (A-7) or (A-8) will be required for determining δ whenever the study area ratio X/Y is equal to the average of the ratios of two equally commensurate lattices. The above examples bear out this relationship.

APPENDIX B **UNIT LATTICE AVERAGE EUCLIDEAN DISTANCE VALUES**

Dimensions of Sublattice 100 by 100			Average Distance		
A	C				
2	2	1.12500	2	66	21.06670
2	3	1.40000	2	67	22.10707
2	4	1.70000	2	68	22.85000
2	5	2.02500	2	69	23.00000
2	6	2.37500	2	70	23.50000
2	7	2.75000	2	71	23.90000
2	8	3.15000	2	72	24.10000
2	9	3.57500	2	73	24.20000
2	10	4.02500	2	74	24.20000
2	11	4.50000	2	75	24.10000
2	12	4.97500	2	76	23.90000
2	13	5.45000	2	77	23.60000
2	14	5.92500	2	78	23.20000
2	15	6.40000	2	79	22.70000
2	16	6.87500	2	80	22.10000
2	17	7.35000	2	81	21.40000
2	18	7.82500	2	82	20.60000
2	19	8.30000	2	83	19.70000
2	20	8.77500	2	84	18.70000
2	21	9.25000	2	85	17.60000
2	22	9.72500	2	86	16.40000
2	23	10.20000	2	87	15.10000
2	24	10.67500	2	88	13.70000
2	25	11.15000	2	89	12.20000
2	26	11.62500	2	90	10.60000
2	27	12.10000	2	91	8.90000
2	28	12.57500	2	92	7.10000
2	29	13.05000	2	93	5.20000
2	30	13.52500	2	94	3.20000
2	31	14.00000	2	95	1.10000
2	32	14.47500	2	96	0.00000
2	33	14.95000	2	97	0.00000
2	34	15.42500	2	98	0.00000
2	35	15.90000	2	99	0.00000
2	36	16.37500	2	100	0.00000
2	37	16.85000	2	101	0.00000
2	38	17.32500	2	102	0.00000
2	39	17.80000	2	103	0.00000
2	40	18.27500	2	104	0.00000
2	41	18.75000	2	105	0.00000
2	42	19.22500	2	106	0.00000
2	43	19.70000	2	107	0.00000
2	44	20.17500	2	108	0.00000
2	45	20.65000	2	109	0.00000
2	46	21.12500	2	110	0.00000
2	47	21.60000	2	111	0.00000
2	48	22.07500	2	112	0.00000
2	49	22.55000	2	113	0.00000
2	50	23.02500	2	114	0.00000
2	51	23.50000	2	115	0.00000
2	52	23.97500	2	116	0.00000
2	53	24.45000	2	117	0.00000
2	54	24.92500	2	118	0.00000
2	55	25.40000	2	119	0.00000
2	56	25.87500	2	120	0.00000
2	57	26.35000	2	121	0.00000
2	58	26.82500	2	122	0.00000
2	59	27.30000	2	123	0.00000
2	60	27.77500	2	124	0.00000
2	61	28.25000	2	125	0.00000
2	62	28.72500	2	126	0.00000
2	63	29.20000	2	127	0.00000
2	64	29.67500	2	128	0.00000
2	65	30.15000	2	129	0.00000
2	66	30.62500	2	130	0.00000
2	67	31.10000	2	131	0.00000
2	68	31.57500	2	132	0.00000
2	69	32.05000	2	133	0.00000
2	70	32.52500	2	134	0.00000
2	71	33.00000	2	135	0.00000
2	72	33.47500	2	136	0.00000
2	73	33.95000	2	137	0.00000
2	74	34.42500	2	138	0.00000
2	75	34.90000	2	139	0.00000
2	76	35.37500	2	140	0.00000
2	77	35.85000	2	141	0.00000
2	78	36.32500	2	142	0.00000
2	79	36.80000	2	143	0.00000
2	80	37.27500	2	144	0.00000
2	81	37.75000	2	145	0.00000
2	82	38.22500	2	146	0.00000
2	83	38.70000	2	147	0.00000
2	84	39.17500	2	148	0.00000
2	85	39.65000	2	149	0.00000
2	86	40.12500	2	150	0.00000
2	87	40.60000	2	151	0.00000
2	88	41.07500	2	152	0.00000
2	89	41.55000	2	153	0.00000
2	90	42.02500	2	154	0.00000
2	91	42.50000	2	155	0.00000
2	92	42.97500	2	156	0.00000
2	93	43.45000	2	157	0.00000
2	94	43.92500	2	158	0.00000
2	95	44.40000	2	159	0.00000
2	96	44.87500	2	160	0.00000
2	97	45.35000	2	161	0.00000
2	98	45.82500	2	162	0.00000
2	99	46.30000	2	163	0.00000
2	100	46.77500	2	164	0.00000
2	101	47.25000	2	165	0.00000
2	102	47.72500	2	166	0.00000
2	103	48.20000	2	167	0.00000
2	104	48.67500	2	168	0.00000
2	105	49.15000	2	169	0.00000
2	106	49.62500	2	170	0.00000
2	107	50.10000	2	171	0.00000
2	108	50.57500	2	172	0.00000
2	109	51.05000	2	173	0.00000
2	110	51.52500	2	174	0.00000
2	111	52.00000	2	175	0.00000
2	112	52.47500	2	176	0.00000
2	113	52.95000	2	177	0.00000
2	114	53.42500	2	178	0.00000
2	115	53.90000	2	179	0.00000
2	116	54.37500	2	180	0.00000
2	117	54.85000	2	181	0.00000
2	118	55.32500	2	182	0.00000
2	119	55.80000	2	183	0.00000
2	120	56.27500	2	184	0.00000
2	121	56.75000	2	185	0.00000
2	122	57.22500	2	186	0.00000
2	123	57.70000	2	187	0.00000
2	124	58.17500	2	188	0.00000
2	125	58.65000	2	189	0.00000
2	126	59.12500	2	190	0.00000
2	127	59.60000	2	191	0.00000
2	128	60.07500	2	192	0.00000
2	129	60.55000	2	193	0.00000
2	130	61.02500	2	194	0.00000
2	131	61.50000	2	195	0.00000
2	132	61.97500	2	196	0.00000
2	133	62.45000	2	197	0.00000
2	134	62.92500	2	198	0.00000
2	135	63.40000	2	199	0.00000
2	136	63.87500	2	200	0.00000
2	137	64.35000	2	201	0.00000
2	138	64.82500	2	202	0.00000
2	139	65.30000	2	203	0.00000
2	140	65.77500	2	204	0.00000
2	141	66.25000	2	205	0.00000
2	142	66.72500	2	206	0.00000
2	143	67.20000	2	207	0.00000
2	144	67.67500	2	208	0.00000
2	145	68.15000	2	209	0.00000
2	146	68.62500	2	210	0.00000
2	147	69.10000	2	211	0.00000
2	148	69.57500	2	212	0.00000
2	149	70.05000	2	213	0.00000
2	150	70.52500	2	214	0.00000
2	151	71.00000	2	215	0.00000
2	152	71.47500	2	216	0.00000
2	153	71.95000	2	217	0.00000
2	154	72.42500	2	218	0.00000
2	155	72.90000	2	219	0.00000
2	156	73.37500	2	220	0.00000
2	157	73.85000	2	221	0.00000
2	158	74.32500	2	222	0.00000
2	159	74.80000	2	223	0.00000
2	160	75.27500	2	224	0.00000
2	161	75.75000	2	225	0.00000
2	162	76.22500	2	226	0.00000
2	163	76.70000	2	227	0.00000
2	164	77.17500	2	228	0.00000
2	165	77.65000	2	229	0.00000
2	166	78.12500	2	230	0.00000
2	167	78.60000	2	231	0.00000
2	168	79.07500	2	232	0.00000
2	169	79.55000	2	233	0.00000
2	170	80.02500	2	234	0.00000
2	171	80.50000	2	235	0.00000
2	172	80.97500	2	236	0.00000
2	173	81.45000	2	237	0.00000
2	174	81.92500	2	238	0.00000
2	175	82.40000	2	239	0.00000
2	176	82.87500	2	240	0.00000
2	177	83.35000	2	241	0.00000
2	178	83.82500	2	242	0.00000
2	179	84.30000	2	243	0.00000
2	180	84.77500	2	244	0.00000
2	181	85.25000	2	245	0.00000
2	182	85.72500	2	246	0.00000
2	183	86.20000	2	247	0.00000
2	184	86.67500	2	248	0.00000
2	185	87.15000	2	249	0.00000
2	186	87.62500	2	250	0.00000
2	187	88.10000	2	251	0.00000
2	188	88.57500	2	252	0.00000
2	189	89.05000	2	253	0.00000
2	190	89.52500	2	254	0.00000
2	191	90.00000	2	255	0.00000
2	192	90.47500	2	256	0.00000
2	193	90.95000	2	257	0.00000
2	194	91.42500	2	258	0.00000
2	195	91.90000	2	259	0.00000
2	196	92.37500	2	260	0.00000
2	197	92.85000	2	261	0.00000
2	198	93.32500	2	262	0.00000
2	199	93.80000	2	263	0.00000
2	200	94.27500	2	264	0.00000
2	201	94.75000	2	265	0.00000
2	202	95.22500	2	266	0.00000
2	203	95.70000	2	267	0.00000
2	204	96.17500	2	268	0.00000
2	205	96.65000	2	269	0.00000
2	206	97.12500	2	270	0.00000
2	207	97.60000	2	271	0.00000
2	208	98.07500	2	272	0.00000
2	209	98.55000	2	273	0.00000
2	210	99.02500	2	274	0.00000
2	211	99.50000	2	275	0.00000
2	212	99.97500	2	276	0.00000
2	213	100.45000	2	277	0.00000

4	60	22.80240	5	30	13.62027
4	69	23.21420	5	39	13.26103
4	70	23.54634	5	40	13.60230
4	71	23.87823	5	41	14.01733
4	72	24.21135	5	42	14.34045
4	73	24.54240	5	43	14.67054
4	74	24.87440	5	44	15.00450
4	75	25.20630	5	45	15.33270
4	76	25.53672	5	46	15.66312
4	77	25.87006	5	47	15.99550
4	78	26.20297	5	48	16.32215
4	79	26.53530	5	49	16.65191
4	80	26.86731	5	50	16.98174
4	81	27.19976	5	51	17.31160
4	82	27.53204	5	52	17.64170
4	83	27.86434	5	53	17.97100
4	84	28.19666	5	54	18.30021
4	85	28.52900	5	55	18.62944
4	86	28.86130	5	56	18.95860
4	87	29.19375	5	57	19.28780
4	88	29.52613	5	58	19.61693
4	89	29.85854	5	59	19.94607
4	90	30.19097	5	60	20.27520
4	91	30.52341	5	61	20.60430
4	92	30.85586	5	62	20.93340
4	93	31.18830	5	63	21.26250
4	94	31.52080	5	64	21.59160
4	95	31.85334	5	65	21.92070
4	96	32.18586	5	66	22.24980
4	97	32.51842	5	67	22.57890
4	98	32.85097	5	68	22.90800
4	99	33.18353	5	69	23.23710
4	100	33.51611	5	70	23.56620
5	3	2.63371	5	71	23.89530
5	4	2.81777	5	72	24.22440
5	5	3.13364	5	73	24.55350
5	6	3.47825	5	74	24.88260
5	7	3.74989	5	75	25.21170
5	8	4.06625	5	76	25.54080
5	9	4.30721	5	77	25.86990
5	10	4.67171	5	78	26.19900
5	11	4.87915	5	79	26.52810
5	12	5.22009	5	80	26.85720
5	13	5.68115	5	81	27.18630
5	14	5.91804	5	82	27.51540
5	15	6.23632	5	83	27.84450
5	16	6.54740	5	84	28.17360
5	17	6.90350	5	85	28.50270
5	18	7.18460	5	86	28.83180
5	19	7.50483	5	87	29.16090
5	20	7.82506	5	88	29.49000
5	21	8.16764	5	89	29.81910
5	22	8.47814	5	90	30.14820
5	23	8.79320	5	91	30.47730
5	24	9.11390	5	92	30.80640
5	25	9.44123	5	93	31.13550
5	26	9.76896	5	94	31.46460
5	27	10.09213	5	95	31.79370
5	28	10.41771	5	96	32.12280
5	29	10.74287	5	97	32.45190
5	30	11.06897	5	98	32.78100
5	31	11.39500	5	99	33.11010
5	32	11.72233	5	100	33.43920
5	33	12.04971	6	7	3.16413
5	34	12.37721	6	8	3.43206
5	35	12.70433	6	9	3.70072
6	9	3.90714	6	75	23.21411
6	10	4.27479	6	76	23.54322
6	11	4.50731	6	77	23.87230
6	12	4.86405	6	78	24.20140
6	13	5.16494	6	79	24.53050
6	14	5.46040	6	80	24.85960
6	15	5.77456	6	81	25.18870
6	16	6.08371	6	82	25.51780
6	17	6.39333	6	83	25.84690
6	18	6.70630	6	84	26.17600
6	19	7.02080	6	85	26.50510
6	20	7.33270	6	86	26.83420
6	21	7.64920	6	87	27.16330
6	22	7.96717	6	88	27.49240
6	23	8.28540	6	89	27.82150
6	24	8.60432	6	90	28.15060
6	25	8.92405	6	91	28.47970
6	26	9.24512	6	92	28.80880
6	27	9.56647	6	93	29.13790
6	28	9.88843	6	94	29.46700
6	29	10.21097	6	95	29.79610
6	30	10.53404	6	96	30.12520
6	31	10.85750	6	97	30.45430
6	32	11.18130	6	98	30.78340
6	33	11.50502	6	99	31.11250
6	34	11.82963	6	100	31.44160
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6	37	12.78220	7	9	3.67584
6	38	13.10340	7	10	4.01154
6	39	13.42080	7	11	4.34724
6	40	13.74637	7	12	4.68294
6	41	14.11140	7	13	5.01864
6	42	14.48064	7	14	5.35434
6	43	14.76491	7	15	5.69004
6	44	15.09830	7	16	6.02574
6	45	15.42397	7	17	6.36144
6	46	15.75133	7	18	6.69714
6	47	16.07907	7	19	7.03284
6	48	16.40777	7	20	7.36854
6	49	16.73634	7	21	7.70424
6	50	17.06480	7	22	8.03994
6	51	17.39320	7	23	8.37564
6	52	17.72231	7	24	8.71134
6	53	18.05134	7	25	9.04704
6	54	18.38040	7	26	9.38274
6	55	18.70997	7	27	9.71844
6	56	19.03920	7	28	10.05414
6	57	19.36840	7	29	10.38984
6	58	19.69844	7	30	10.72554
6	59	20.02814	7	31	11.06124
6	60	20.35794	7	32	11.39694
6	61	20.68702	7	33	11.73264
6	62	21.01700	7	34	12.06834
6	63	21.34704	7	35	12.40404
6	64	21.67700	7	36	12.73974
6	65	22.00621	7	37	13.07544
6	66	22.33601	7	38	13.41114
6	67	22.66607	7	39	13.74684
6	68	22.99631	7	40	14.08254
6	69	23.32691	7	41	14.41824
6	70	23.65630	7	42	14.75394
6	71	23.98610	7	43	15.08964
6	72	24.31700	7	44	15.42534
6	73	24.64840	7	45	15.76104
6	74	24.98320	7	46	16.09674

7	47	14.17982	8	20	7.47843
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7	49	14.33394	8	22	6.23861
7	50	17.14124	8	23	6.08644
7	51	17.46677	8	24	6.31473
7	52	17.81643	8	25	9.33194
7	53	18.14426	8	26	9.54634
7	54	18.47225	8	27	9.88149
7	55	18.80034	8	28	10.17763
7	56	19.12846	8	29	10.49439
7	57	19.45707	8	30	10.83231
7	58	19.78642	8	31	11.13674
7	59	20.11429	8	32	11.42982
7	60	20.44209	8	33	11.70982
7	61	20.77000	8	34	12.00979
7	62	21.10182	8	35	12.31209
7	63	21.43813	8	36	12.73189
7	64	21.78034	8	37	13.08944
7	65	22.06671	8	38	13.37577
7	66	22.41812	8	39	13.69449
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7	68	23.07726	8	41	14.34484
7	69	23.46636	8	42	14.68961
7	70	23.73672	8	43	14.89867
7	71	24.06687	8	44	15.31764
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7	73	24.73634	8	46	15.86448
7	74	25.06637	8	47	16.29184
7	75	25.36672	8	48	16.41723
7	76	25.71634	8	49	16.54882
7	77	26.06720	8	50	17.38884
7	78	26.37754	8	51	17.58611
7	79	26.78733	8	52	17.82147
7	80	27.08836	8	53	18.34683
7	81	27.38836	8	54	18.57479
7	82	27.69947	8	55	18.90171
7	83	28.03949	8	56	19.23842
7	84	28.36674	8	57	19.58489
7	85	28.69144	8	58	19.88332
7	86	29.02225	8	59	20.21119
7	87	29.35307	8	60	20.33643
7	88	29.64394	8	61	20.66479
7	89	30.01488	8	62	21.18471
7	90	30.34888	8	63	21.52884
7	91	30.67679	8	64	21.82111
7	92	31.06743	8	65	22.17949
7	93	31.33891	8	66	22.58739
7	94	31.67882	8	67	22.63640
7	95	32.06117	8	68	22.16832
7	96	32.33234	8	69	22.48814
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7	98	32.99485	8	71	24.18390
7	99	33.32814	8	72	24.48129
7	100	33.68747	8	73	24.81040
8	9	4.28814	8	74	25.13689
8	10	4.46341	8	75	25.46897
8	11	4.73636	8	76	25.79633
8	12	5.01341	8	77	26.13884
8	13	5.29848	8	78	26.48744
8	14	5.58281	8	79	26.78734
8	15	5.87248	8	80	27.11712
8	16	6.16829	8	81	27.44636
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8	18	6.77384	8	83	28.10881
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8	95	32.07833	9	95	32.88016
8	96	32.40149	9	96	32.91821
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9	19	7.58722	9	19	7.58722
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9	24	9.08490	9	24	9.08490
9	25	9.48841	9	25	9.48841
9	26	9.71482	9	26	9.71482
9	27	10.02833	9	27	10.02833
9	28	10.34884	9	28	10.34884
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9	32	11.60134	9	32	11.60134
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9	37	13.18088	9	37	13.18088
9	38	13.51382	9	38	13.51382
9	39	13.83448	9	39	13.83448
9	40	14.18882	9	40	14.18882
9	41	14.47783	9	41	14.47783
9	42	14.78844	9	42	14.78844
9	43	15.12123	9	43	15.12123
9	44	15.44389	9	44	15.44389
9	45	15.76689	9	45	15.76689
9	46	16.09923	9	46	16.09923
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9	69	22.88016	9	69	22.88016
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9	79	26.87815	9	79	26.87815
9	80	27.20421	9	80	27.20421
9	81	27.53331	9	81	27.53331
9	82	27.86236	9	82	27.86236
9	83	28.19176	9	83	28.19176
9	84	28.52119	9	84	28.52119
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9	86	29.18049	9	86	29.18049
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9	94	31.81822	9	94	31.81822
9	95	32.14826	9	95	32.14826
9	96	32.47834	9	96	32.47834
9	97	32.80831	9	97	32.80831
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9	99	33.06897	9	99	33.06897
9	100	33.79826	9	100	33.79826
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10	33	12.39888	10	33	12.39888
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10	30	12.90005	11	15	6.90025
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10	36	14.70011	11	21	8.70055
10	37	15.00012	11	22	9.00060
10	38	15.30013	11	23	9.30065
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10	40	15.90015	11	25	9.90075
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10	42	16.50017	11	27	10.50085
10	43	16.80018	11	28	10.80090
10	44	17.10019	11	29	11.10095
10	45	17.40020	11	30	11.40100
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17	158	-10.06200	17	224	-12.02650
17	159	-10.29600	17	225	-12.27595
17	160	-10.53000	17	226	-12.52040
17	161	-10.76400	17	227	-12.75985
17	162	-10.99800	17	228	-12.99430
17	163	-			

19	33	19.80042	20	30	18.81164
19	34	20.19113	20	39	18.80066
19	35	20.50230	20	40	16.10677
19	36	20.01417	20	41	16.40091
19	37	21.13645	20	42	16.70005
19	38	21.43021	20	43	17.00713
19	39	21.73544	20	44	17.30011
19	40	22.04011	20	45	17.61186
19	41	22.30022	20	46	17.91843
19	42	22.60474	20	47	18.22009
19	43	22.90907	20	48	18.52530
19	44	23.22490	20	49	18.83125
19	45	23.54049	20	50	19.13789
19	46	23.86475	20	51	19.44519
19	47	24.17910	20	52	19.75314
19	48	24.50091	20	53	20.06171
19	49	24.80700	20	54	20.37067
19	50	25.22440	20	55	20.68000
19	51	25.54212	20	56	20.99000
19	52	25.86013	20	57	21.30109
19	53	26.17944	20	58	21.61381
19	54	26.49783	20	59	21.92443
19	55	26.81589	20	60	22.23712
19	56	27.13503	20	61	22.54904
19	57	27.45441	20	62	22.86305
19	58	27.77404	20	63	23.17687
19	59	28.09394	20	64	23.49079
19	60	28.41400	20	65	23.80513
19	61	28.73441	20	66	24.11995
19	62	29.05499	20	67	24.43514
19	63	29.37579	20	68	24.75049
19	64	29.69679	20	69	25.06489
19	65	30.01801	20	70	25.38284
19	66	30.33942	20	71	25.69941
19	67	30.66103	20	72	26.01530
19	68	30.98284	20	73	26.33351
19	69	31.30482	20	74	26.65101
19	70	31.62699	20	75	26.96801
19	71	31.94934	20	76	27.28499
19	72	32.27184	20	77	27.60234
19	73	32.59454	20	78	27.92004
19	74	32.91740	20	79	28.24274
19	75	33.24041	20	80	28.56100
19	76	33.56357	20	81	28.88126
19	77	33.88689	20	82	29.20000
19	78	34.21036	20	83	29.52073
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19	80	34.85773	20	85	30.16111
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20	23	11.23676	20	89	31.44439
20	24	11.50773	20	90	31.76571
20	25	11.78127	20	91	32.08723
20	26	12.05722	20	92	32.40991
20	27	12.33643	20	93	32.73076
20	28	12.61879	20	94	33.05282
20	29	12.89404	20	95	33.37504
20	30	13.18224	20	96	33.69742
20	31	13.46815	20	97	34.01997
20	32	13.75176	20	98	34.34307
20	33	14.04494	20	99	34.66553
20	34	14.33642	20	100	34.98855
20	35	14.62769	21	21	19.90204
20	36	14.92110	21	22	13.20405
20	37	15.21577	21	23	11.40010

21	24	11.70499	21	90	31.90033
21	25	12.02733	21	91	32.22099
21	26	12.30088	21	92	32.54904
21	27	12.57890	21	93	32.87600
21	28	12.86044	21	94	33.19211
21	29	13.13503	21	95	33.51182
21	30	13.41436	21	96	33.83011
21	31	13.69791	21	97	34.15007
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21	33	14.26970	21	99	34.79000
21	34	14.55878	21	100	35.12316
21	35	14.84767	22	22	11.40290
21	36	15.13676	22	23	11.70405
21	37	15.43121	22	24	12.00972
21	38	15.72409	22	25	12.27722
21	39	16.01977	22	26	12.54747
21	40	16.31870	22	27	12.82001
21	41	16.61200	22	28	13.09400
21	42	16.91101	22	29	13.37172
21	43	17.21013	22	30	13.65063
21	44	17.51020	22	31	13.93163
21	45	17.81117	22	32	14.21401
21	46	18.11300	22	33	14.49820
21	47	18.41564	22	34	14.78416
21	48	18.71913	22	35	15.07153
21	49	19.02354	22	36	15.36030
21	50	19.32839	22	37	15.65059
21	51	19.63394	22	38	15.94299
21	52	19.94029	22	39	16.23404
21	53	20.24724	22	40	16.52677
21	54	20.55484	22	41	16.82104
21	55	20.86304	22	42	17.11990
21	56	21.17182	22	43	17.41715
21	57	21.48110	22	44	17.71550
21	58	21.79103	22	45	18.01400
21	59	22.10162	22	46	18.31400
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21	67	24.60125	22	54	20.72804
21	68	24.91560	22	55	21.04031
21	69	25.23031	22	56	21.35070
21	70	25.54539	22	57	21.66404
21	71	25.86081	22	58	21.97307
21	72	26.17657	22	59	22.28204
21	73	26.49264	22	60	22.59133
21	74	26.80907	22	61	22.90154
21	75	27.12576	22	62	23.21203
21	76	27.44280	22	63	23.52300
21	77	27.76011	22	64	23.83443
21	78	28.07770	22	65	24.14631
21	79	28.39567	22	66	24.45861
21	80	28.71371	22	67	24.77134
21	81	29.03210	22	68	25.08440
21	82	29.35076	22	69	25.39794
21	83	29.66965	22	70	25.71197
21	84	29.98879	22	71	26.02614
21	85	30.30816	22	72	26.34076
21	86	30.62776	22	73	26.65572
21	87	30.94759	22	74	26.97103
21	88	31.26762	22	75	27.28666
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22	79	28.53226	23	67	24.94522
22	80	28.84939	23	68	25.25712
22	81	29.16779	23	69	25.56943
22	82	29.48447	23	70	25.88214
22	83	29.80240	23	71	26.19524
22	84	30.10889	23	72	26.50871
22	85	30.41902	23	73	26.82255
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22	89	31.72812	23	77	28.08133
22	90	32.06470	23	78	28.39684
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23	31	14.16832	23	97	34.44160
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23	45	18.22146	24	34	15.24734
23	46	18.51963	24	35	15.53013
23	47	18.81871	24	36	15.81480
23	48	19.11866	24	37	16.10031
23	49	19.41943	24	38	16.38782
23	50	19.72101	24	39	16.67687
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23	52	20.32643	24	41	17.26181
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23	62	23.39238	24	51	20.22364
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24	54	21.13021	25	44	19.38277
24	55	21.43381	25	45	19.64681
24	56	21.73897	25	46	19.90904
24	57	22.04597	25	47	19.23048
24	58	22.35469	25	48	19.53264
24	59	22.66460	25	49	19.83613
24	60	22.96129	25	50	20.13940
24	61	23.26554	25	51	20.43745
24	62	23.57633	25	52	20.73262
24	63	23.88443	25	53	21.02790
24	64	24.19344	25	54	21.32325
24	65	24.50274	25	55	21.61812
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24	68	25.43341	25	58	22.50156
24	69	25.74452	25	59	22.84624
24	70	26.05604	25	60	23.15153
24	71	26.36796	25	61	23.45789
24	72	26.68028	25	62	23.76362
24	73	26.99299	25	63	24.07079
24	74	27.30606	25	64	24.37829
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24	76	27.93327	25	66	24.99479
24	77	28.24740	25	67	25.30577
24	78	28.56185	25	68	25.61321
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24	80	29.19172	25	70	26.23342
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24	83	30.13879	25	73	27.16690
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24	86	31.08840	25	76	28.10394
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24	88	31.72279	25	78	28.73021
24	89	32.04036	25	79	29.04404
24	90	32.35817	25	80	29.35810
24	91	32.67622	25	81	29.67240
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24	94	33.63172	25	84	30.61747
24	95	33.95067	25	85	30.93308
24	96	34.26991	25	86	31.24891
24	97	34.58917	25	87	31.56504
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24	99	35.22847	25	89	32.19810
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25	23	13.04572	25	91	32.83219
25	24	13.36784	25	92	33.14959
25	25	13.67197	25	93	33.46723
25	26	13.98001	25	94	33.78510
25	27	14.10794	25	95	34.10320
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25	29	14.65389	25	97	34.74006
25	30	14.92780	25	98	35.05880
25	31	15.20063	25	99	35.37775
25	32	15.48392	25	100	35.69690
25	33	15.76646	26	26	13.94673
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25	37	16.89618	26	30	15.22820
25	38	17.18093	26	31	15.54922
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25	40	17.76890	26	33	16.19699
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26	28	16.84422	27	30	14.88012
26	29	17.13004	27	31	15.14049
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26	33	18.28144	27	35	16.20236
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26	35	18.86377	27	37	16.70984
26	36	19.15652	27	38	17.00051
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26	38	19.74500	27	40	17.56666
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26	43	21.23196	27	45	19.00439
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26	68	28.90229	27	70	26.59814
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26	72	30.15465	27	74	27.83432
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27	42	38.57168	28	43	36.47748
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27	63	45.40436	28	64	43.17832
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27	68	47.04576	28	69	44.78752
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27	71	48.03276	28	72	45.75544
27	72	48.36216	28	73	46.07848
27	73	48.69176	28	74	46.40172
27	74	49.02156	28	75	46.72516
27	75	49.35156	28	76	47.04880
27	76	49.68176	28	77	47.37264
27	77	50.01216	28	78	47.69668
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27	80	51.00456	28	81	48.66992
27	81	51.33576	28	82	48.99468
27	82	51.66716	28	83	49.31964
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27	85	52.66256	28	86	50.29572
27	86	52.99476	28	87	50.62148
27	87	53.32716	28	88	50.94744
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20	92	23.80131	30	87	22.40047
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20	94	24.42394	30	89	23.00363
20	95	24.74454	30	90	23.34899
20	96	25.06944	30	91	23.63044
20	97	25.37407	30	92	23.97160
20	98	25.69012	30	93	24.25408
20	99	26.00611	30	94	24.59436
20	100	26.32173	30	95	24.91219
30	30	15.68103	30	96	25.22628
30	31	15.91271	30	97	25.54043
30	32	16.17658	30	98	25.85524
30	33	16.44844	30	99	26.17010
30	34	16.71829	30	100	26.48522
30	35	16.98002	31	31	16.17216
30	36	17.25153	31	32	16.43381
30	37	17.52074	31	33	16.69783
30	38	17.79989	31	34	16.96329
30	39	18.07690	31	35	17.23083
30	40	18.35390	31	36	17.50040
30	41	18.63224	31	37	17.77160
30	42	18.91395	31	38	18.04447
30	43	19.19899	31	39	18.31893
30	44	19.47929	31	40	18.59482
30	45	19.76380	31	41	18.87238
30	46	20.04949	31	42	19.15124
30	47	20.33630	31	43	19.43144
30	48	20.62420	31	44	19.71287
30	49	20.91314	31	45	19.99572
30	50	21.20309	31	46	20.27968
30	51	21.49401	31	47	20.56479
30	52	21.78596	31	48	20.85101
30	53	22.07802	31	49	21.13830
30	54	22.37223	31	50	21.42662
30	55	22.66672	31	51	21.71594
30	56	22.96201	31	52	22.00623
30	57	23.25808	31	53	22.29744
30	58	23.55491	31	54	22.58954
30	59	23.85240	31	55	22.88251
30	60	24.15077	31	56	23.17632
30	61	24.44974	31	57	23.47094
30	62	24.74939	31	58	23.76634
30	63	25.04968	31	59	24.06250
30	64	25.35060	31	60	24.35940
30	65	25.65213	31	61	24.65700
30	66	25.95426	31	62	24.95530
30	67	26.25698	31	63	25.25426
30	68	26.56021	31	64	25.55388
30	69	26.86401	31	65	25.85412
30	70	27.16833	31	66	26.15497
30	71	27.47316	31	67	26.45641
30	72	27.77849	31	68	26.75843
30	73	28.08431	31	69	27.06101
30	74	28.39059	31	70	27.36413
31	71	27.68770	32	60	26.96336
31	72	27.97194	32	61	27.26072
31	73	28.27600	32	62	27.56264
31	74	28.58173	32	63	27.86811
31	75	28.88737	32	64	28.16810
31	76	29.19345	32	65	28.47141
31	77	29.49984	32	66	28.77542
31	78	29.80658	32	67	29.08012
31	79	30.11424	32	68	29.38610
31	80	30.42215	32	69	29.69453
31	81	30.73033	32	70	29.99642
31	82	31.03894	32	71	30.30275
31	83	31.34794	32	72	30.60950
31	84	31.65731	32	73	30.91668
31	85	31.96703	32	74	31.22426
31	86	32.27712	32	75	31.53223
31	87	32.58753	32	76	31.84060
31	88	32.89822	32	77	32.14934
31	89	33.20942	32	78	32.45843
31	90	33.52086	32	79	32.76782
31	91	33.83260	32	80	33.07774
31	92	34.14463	32	81	33.38791
31	93	34.45701	32	82	33.69841
31	94	34.76964	32	83	34.00924
31	95	35.08260	32	84	34.32039
31	96	35.39583	32	85	34.63185
31	97	35.70933	32	86	34.94362
31	98	36.02310	32	87	35.25569
31	99	36.33713	32	88	35.56806
31	100	36.65143	32	89	35.88069
32	32	16.63330	32	90	36.19362
32	33	16.95493	32	91	36.50682
32	34	17.21659	32	100	36.82029
32	35	17.48417	33	33	17.21446
32	36	17.75162	33	34	17.47604
32	37	18.02004	33	35	17.73963
32	38	18.29173	33	36	18.00699
32	39	18.56429	33	37	18.27234
32	40	18.83639	33	38	18.54133
32	41	19.11399	33	39	18.81197
32	42	19.39102	33	40	19.08420
32	43	19.66943	33	41	19.35794
32	44	19.94917	33	42	19.63318
32	45	20.23018	33	43	19.90900
32	46	20.51241	33	44	20.18770
32	47	20.79583	33	45	20.46787
32	48	21.08039	33	46	20.74760
32	49	21.36605	33	47	21.02925
32	50	21.65274	33	48	21.31226
32	51	21.94049	33	49	21.59629
32	52	22.22921	33	50	21.88140
32	53	22.51888	33	51	22.16784
32	54	22.80947	33	52	22.45472
32	55	23.10095	33	53	22.74297
32	56	23.39329	33	54	23.03195
32	57	23.68646	33	55	23.32195
32	58	23.98044	33	56	23.61282
32	59	24.27519	33	57	23.90458
32	60	24.57071	33	58	24.19711
32	61	24.86698	33	59	24.49047
32	62	25.16390	33	60	24.78460
32	63	25.46154	33	61	25.07940
32	64	25.75984	33	62	25.37589
32	65	26.05880	33	63	25.67311
32	66	26.35830	33	64	25.96942
32	67	26.65857	33	65	26.26699

23	66	26.54444	34	63	26.47869
23	67	26.54335	34	64	26.77295
23	68	27.18290	34	65	27.67043
23	69	27.64306	34	66	27.34897
23	70	27.76377	34	67	27.66781
23	71	26.96385	34	68	27.96744
23	72	26.54404	34	69	28.26754
23	73	26.54824	34	70	28.54420
23	74	26.67212	34	71	28.86941
23	75	29.27530	34	72	29.17116
23	76	29.57937	34	73	29.47341
23	77	29.64371	34	74	29.77518
23	78	26.18482	34	75	29.67943
23	79	26.48376	34	76	29.38316
23	80	26.79949	34	77	29.68736
23	81	21.18682	34	78	29.98862
23	82	21.43219	34	79	21.29712
23	83	21.71814	34	80	21.68865
23	84	22.62681	34	81	21.98669
23	85	22.33426	34	82	22.21496
23	86	22.64246	34	83	22.52173
23	87	22.95091	34	84	22.82869
23	88	23.25875	34	85	23.13643
23	89	23.56590	34	86	23.44425
23	90	23.87357	34	87	23.75263
23	91	24.18049	34	88	24.06129
23	92	24.48673	34	89	24.37027
23	93	24.79329	34	90	24.67940
23	94	25.12610	34	91	24.98927
23	95	25.43137	34	92	25.29926
23	96	25.74284	34	93	25.60937
23	97	26.06463	34	94	25.92029
23	98	26.34673	34	95	26.23113
23	99	26.67910	34	96	26.54236
23	100	26.99174	34	97	26.85369
34	34	17.73564	34	100	37.18370
34	35	17.59721	35	35	18.26462
34	36	16.26670	35	36	18.51830
34	37	16.52663	35	37	18.76179
34	38	16.78311	35	38	19.04699
34	39	19.04187	35	39	19.31391
34	40	19.32265	35	40	19.58246
34	41	19.60419	35	41	19.85260
34	42	19.87762	35	42	20.12426
34	43	20.15244	35	43	20.39737
34	44	20.42872	35	44	20.67189
34	45	20.70630	35	45	20.94777
34	46	20.98515	35	46	21.22495
34	47	21.26323	35	47	21.50339
34	48	21.54630	35	48	21.78304
34	49	21.82882	35	49	22.06386
34	50	22.11244	35	50	22.34511
34	51	22.39784	35	51	22.62685
34	52	22.68266	35	52	22.91285
34	53	22.96929	35	53	23.19896
34	54	23.25686	35	54	23.48416
34	55	23.54540	35	55	23.77122
34	56	23.83402	35	56	24.05920
34	57	24.12512	35	57	24.34807
34	58	24.41626	35	58	24.63781
34	59	24.70623	35	59	24.92839
34	60	25.00090	35	60	25.21979
34	61	25.29482	35	61	25.51197
34	62	25.58879	35	62	25.80482
34	63	25.88380	35	63	26.09841
34	64	26.17986	35	64	26.39362
26	65	26.68614	36	65	27.19729
26	66	27.08394	36	66	27.48251
26	67	27.28639	36	67	27.76839
26	68	27.57749	36	68	28.06491
26	69	27.87522	36	69	28.36286
26	70	26.17584	36	70	28.67381
26	71	26.47248	36	71	28.97815
26	72	26.77196	36	72	29.27767
26	73	29.07286	36	73	29.57933
26	74	29.37264	36	74	29.87637
26	75	29.67268	36	75	30.17713
26	76	29.97246	36	76	30.47341
26	77	30.27762	36	77	30.77378
26	78	30.58029	36	78	31.06186
26	79	30.88341	36	79	31.35441
26	80	31.18782	36	80	31.64743
26	81	31.49184	36	81	31.94091
26	82	31.79634	36	82	32.23484
26	83	32.10032	36	83	32.52921
26	84	32.40589	36	84	32.82400
26	85	32.71156	36	85	33.11929
26	86	33.01785	36	86	33.41462
26	87	33.23443	36	87	33.72082
26	88	33.53139	36	88	34.02722
26	89	33.83673	36	89	34.33486
26	90	34.14044	36	90	34.64115
26	91	34.45451	36	91	34.94664
26	92	34.86233	36	92	35.25452
26	93	35.17170	36	93	35.56474
26	94	35.48086	36	94	35.87323
26	95	35.78924	36	95	36.18217
26	96	36.09999	36	96	36.49134
26	97	36.41067	36	97	36.80051
26	98	36.72045	36	98	37.11073
26	99	37.03113	36	99	37.42090
26	100	37.34211	36	100	37.73023
36	36	16.77182	37	37	19.29923
36	37	19.63934	37	38	19.56674
36	38	19.90290	37	39	19.82462
36	39	19.56796	37	40	20.08899
36	40	19.63474	37	41	20.35860
36	41	20.18210	37	42	20.62377
36	42	20.37390	37	43	20.89345
36	43	20.64439	37	44	21.16459
36	44	20.91721	37	45	21.43712
36	45	21.19141	37	46	21.71201
36	46	21.46489	37	47	21.98650
36	47	21.74374	37	48	22.26233
36	48	22.02170	37	49	22.54032
36	49	22.30182	37	50	22.81916
36	50	22.58141	37	51	23.09913
36	51	22.86291	37	52	23.38020
36	52	23.14540	37	53	23.66233
36	53	23.42910	37	54	23.94549
36	54	23.71373	37	55	24.22963
36	55	23.99833	37	56	24.51477
36	56	24.28387	37	57	24.80002
36	57	24.57333	37	58	25.08777
36	58	24.86167	37	59	25.37941
36	59	25.15086	37	60	25.66429
36	60	25.44091	37	61	25.95306
36	61	25.73176	37	62	26.24411
36	62	26.02336	37	63	26.53529
36	63	26.31577	37	64	26.82706
36	64	26.60890	37	65	27.11943
36	65	26.90274	37	66	27.41292
			37	67	27.70661

37	60	20.00130	30	71	29.10131
37	69	20.22090	30	72	29.39734
37	70	20.50204	30	73	29.69394
37	71	20.60204	30	74	29.99120
37	72	20.10062	30	75	30.28900
37	73	20.40440	30	76	30.58736
37	74	20.70275	30	77	30.88626
37	75	30.00166	30	78	31.18570
37	76	30.00112	30	79	31.48508
37	77	30.00111	30	80	31.78411
37	78	30.00161	30	81	32.08277
37	79	31.28282	30	82	32.38030
37	80	31.58412	30	83	32.67941
37	81	31.88412	30	84	32.97877
37	82	32.18030	30	85	33.27839
37	83	32.48149	30	86	33.57804
37	84	32.78406	30	87	33.87832
37	85	33.08606	30	88	34.17942
37	86	33.38809	30	89	34.48105
37	87	33.70754	30	90	35.12135
37	88	34.01259	30	91	35.42703
37	89	34.31005	30	92	35.73310
37	90	34.62509	30	93	36.03952
37	91	34.93011	30	94	36.34631
37	92	35.23671	30	95	36.65345
37	93	35.54360	30	96	36.96092
37	94	35.85100	30	97	37.26870
37	95	36.15807	30	98	37.57690
37	96	36.46608	30	99	37.88537
37	97	36.77502	30	100	38.19410
37	98	37.08370	39	39	20.34160
37	99	37.39269	39	40	20.64316
37	100	37.70200	39	41	20.94621
38	39	19.82045	39	42	21.25100
38	40	20.00195	39	43	21.55740
38	41	20.24516	39	44	21.86522
38	42	20.41003	39	45	22.17440
38	43	20.67649	39	46	22.48513
38	44	21.10468	39	47	22.79716
38	45	21.41395	39	48	23.10947
38	46	21.68404	39	49	23.42203
38	47	21.93711	39	50	23.73502
38	48	22.23070	39	51	24.04877
38	49	22.52557	39	52	24.36367
38	50	22.82160	39	53	24.67906
38	51	23.05000	39	54	24.99532
38	52	23.27440	39	55	25.31262
38	53	23.49766	39	56	25.63110
38	54	24.17930	39	57	25.95069
38	55	24.46210	39	58	26.27131
38	56	24.74501	39	59	26.59306
38	57	25.02806	39	60	26.91592
38	58	25.31104	39	61	27.23990
38	59	25.60231	39	62	27.56500
38	60	25.89185	39	63	27.89120
38	61	26.17903	39	64	28.21850
38	62	26.46704	39	65	28.54676
38	63	26.75483	39	66	28.87600
38	64	27.04741	39	67	29.20632
38	65	27.33872	39	68	29.53767
38	66	27.63070	39	69	29.87000
38	67	27.92334	39	70	30.20430
38	68	28.21699	39	71	30.54060
38	69	28.51111	39	72	30.87890
38	70	28.80600	39	73	31.21920
			39	74	31.56150

39	75	30.49083	40	80	32.10661
39	76	30.78679	40	81	32.40830
39	77	31.08361	40	82	32.71040
39	78	31.38130	40	83	33.01390
39	79	31.68000	40	84	33.31880
39	80	31.98020	40	85	33.62500
39	81	32.28221	40	86	33.93250
39	82	32.58603	40	87	34.24130
39	83	32.89132	40	88	34.55140
39	84	33.19809	40	89	34.86290
39	85	33.50472	40	90	35.17580
39	86	33.79700	40	91	35.49000
39	87	34.09972	40	92	35.80560
39	88	34.40206	40	93	36.12260
39	89	34.70645	40	94	36.44100
39	90	35.01041	40	95	36.76080
39	91	35.31479	40	96	37.08200
39	92	35.61954	40	97	37.40460
39	93	35.92472	40	98	37.72860
39	94	36.23025	40	99	38.05400
39	95	36.53610	40	100	38.38080
39	96	36.84242	41	41	21.30410
39	97	37.14904	41	42	21.60860
39	98	37.45600	41	43	21.91460
39	99	37.76330	41	44	22.22200
39	100	38.07094	41	45	22.53080
40	40	20.06292	41	46	22.84000
40	41	21.12430	41	47	23.15060
40	42	21.38747	41	48	23.46260
40	43	21.65214	41	49	23.77600
40	44	21.91833	41	50	24.09080
40	45	22.18599	41	51	24.40700
40	46	22.45507	41	52	24.72460
40	47	22.72551	41	53	25.04360
40	48	23.00727	41	54	25.36400
40	49	23.27931	41	55	25.68580
40	50	23.54480	41	56	26.00900
40	51	23.82000	41	57	26.33360
40	52	24.09600	41	58	26.65960
40	53	24.37400	41	59	26.98700
40	54	24.65325	41	60	27.31580
40	55	24.93313	41	61	27.64600
40	56	25.21400	41	62	27.97760
40	57	25.49600	41	63	28.31060
40	58	25.77977	41	64	28.64500
40	59	26.06524	41	65	28.98080
40	60	26.34722	41	66	29.31800
40	61	26.63270	41	67	29.65660
40	62	26.91919	41	68	29.99660
40	63	27.20642	41	69	30.33800
40	64	27.49440	41	70	30.68080
40	65	27.78320	41	71	31.02500
40	66	28.07287	41	72	31.37060
40	67	28.36310	41	73	31.71760
40	68	28.65422	41	74	32.06600
40	69	28.94590	41	75	32.41580
40	70	29.23840	41	76	32.76700
40	71	29.53150	41	77	33.11960
40	72	29.82620	41	78	33.47360
40	73	30.12141	41	79	33.82900
40	74	30.41800	41	80	34.18580
40	75	30.71510	41	81	34.54400
40	76	31.01360	41	82	34.90360
40	77	31.31360	41	83	35.26460
40	78	31.61500	41	84	35.62700
40	79	31.91780	41	85	35.99080

41	86	34.19949	42	83	34.51227
41	87	34.50044	42	84	34.51313
41	88	34.50179	42	85	37.13430
41	89	35.18341	42	86	37.22282
41	90	35.40852	42	87	37.72608
41	91	35.70004	42	88	38.03044
41	92	36.01101	42	89	38.23520
41	93	36.31436	42	100	38.44031
41	94	36.61811	43	43	22.42667
41	95	36.92225	43	44	22.68009
41	96	37.22676	43	45	22.93102
41	97	37.53103	43	46	23.21543
41	98	37.83690	43	47	23.48127
41	99	38.14281	43	48	23.74840
41	100	38.44844	43	49	24.01782
42	42	21.90845	43	50	24.28604
42	43	22.16684	43	51	24.55794
42	44	22.42943	43	52	24.83023
42	45	22.69432	43	53	25.10370
42	46	22.96027	43	54	25.37830
42	47	23.22742	43	55	25.65401
42	48	23.49634	43	56	25.93076
42	49	23.76636	43	57	26.20860
42	50	24.03747	43	58	26.48762
42	51	24.31020	43	59	26.76722
42	52	24.58392	43	60	27.04797
42	53	24.85890	43	61	27.32940
42	54	25.13490	43	62	27.61222
42	55	25.41189	43	63	27.89644
42	56	25.69043	43	64	28.17994
42	57	25.96919	43	65	28.46504
42	58	26.24894	43	66	28.75181
42	59	26.52944	43	67	29.03772
42	60	26.81231	43	68	29.32520
42	61	27.09647	43	69	29.61341
42	62	27.37931	43	70	29.90235
42	63	27.66401	43	71	30.19200
42	64	27.94955	43	72	30.48233
42	65	28.23590	43	73	30.77333
42	66	28.52304	43	74	31.06499
42	67	28.81089	43	75	31.35726
42	68	29.09941	43	76	31.65020
42	69	29.38899	43	77	31.94373
42	70	29.67909	43	78	32.23784
42	71	29.96988	43	79	32.53254
42	72	30.26134	43	80	32.82766
42	73	30.55346	43	81	33.12341
42	74	30.84623	43	82	33.41994
42	75	31.13961	43	83	33.71684
42	76	31.43361	43	84	34.01424
42	77	31.72820	43	85	34.31214
42	78	32.02330	43	86	34.61053
42	79	32.31912	43	87	34.90940
42	80	32.61562	43	88	35.20874
42	81	32.91283	43	89	35.50858
42	82	33.20982	43	90	35.80890
42	83	33.50750	43	91	36.10950
42	84	33.80584	43	92	36.41043
42	85	34.10476	43	93	36.71216
42	86	34.40432	43	94	37.01414
42	87	34.70395	43	95	37.31651
42	88	35.00424	43	96	37.61920
42	89	35.30490	43	97	37.92244
42	90	35.60617	43	98	38.22597
42	91	35.90776	43	99	38.52949
42	92	36.20982	43	100	38.83416
44	44	23.94794	45	54	25.87947
44	45	23.20934	45	55	26.14345
44	46	23.47223	45	56	26.41783
44	47	23.73634	45	57	26.69268
44	48	24.00223	45	58	26.96807
44	49	24.26934	45	59	27.24407
44	50	24.53774	45	60	27.52034
44	51	24.80739	45	61	27.80337
44	52	25.07826	45	62	28.08343
44	53	25.35033	45	63	28.36490
44	54	25.62354	45	64	28.64693
44	55	25.89780	45	65	28.92932
44	56	26.17330	45	66	29.21245
44	57	26.44976	45	67	29.49678
44	58	26.72726	45	68	29.78191
44	59	27.00577	45	69	30.06790
44	60	27.28523	45	70	30.35444
44	61	27.56563	45	71	30.64182
44	62	27.84694	45	72	30.92990
44	63	28.12914	45	73	31.21849
44	64	28.41220	45	74	31.50815
44	65	28.69611	45	75	31.79837
44	66	28.98083	45	76	32.08963
44	67	29.26636	45	77	32.38063
44	68	29.55263	45	78	32.67245
44	69	29.83976	45	79	32.96506
44	70	30.12749	45	80	33.25836
44	71	30.41599	45	81	33.55204
44	72	30.70520	45	82	33.84636
44	73	30.99509	45	83	34.14126
44	74	31.28563	45	84	34.43688
44	75	31.57685	45	85	34.73263
44	76	31.86869	45	86	35.02909
44	77	32.16113	45	87	35.32606
44	78	32.45421	45	88	35.62356
44	79	32.74787	45	89	35.92143
44	80	33.04210	45	90	36.21984
44	81	33.33689	45	91	36.51870
44	82	33.63223	45	92	36.81801
44	83	33.92812	45	93	37.11776
44	84	34.22452	45	94	37.41796
44	85	34.52144	45	95	37.71854
44	86	34.81897	45	96	38.01950
44	87	35.11676	45	97	38.32101
44	88	35.41518	45	98	38.62284
44	89	35.71406	45	99	38.92504
44	90	36.01337	45	100	39.22764
44	91	36.31313	46	46	23.99049
44	92	36.61337	46	47	24.25106
44	93	36.91400	46	48	24.51144
44	94	37.21510	46	49	24.77264
44	95	37.51669	46	50	25.03436
44	96	37.81868	46	51	25.29116
44	97	38.12077	46	52	25.54796
44	98	38.42346	46	53	25.80486
44	99	38.72632	46	54	26.06184
44	100	39.02994	46	55	26.31867
45	45	23.46921	46	56	26.57522
45	46	23.73060	46	57	26.83725
45	47	24.00344	46	58	27.09421
45	48	24.27679	46	59	27.35008
45	49	24.55031	46	60	27.60496
45	50	24.79996	46	61	27.85983
45	51	25.05044	46	62	28.11464
45	52	25.30176	46	63	28.36947
45	53	25.55303	46	64	28.62431

66	65	29.14344	47	77	32.82437
66	66	29.44881	47	78	33.11430
66	67	29.72897	47	79	33.66485
66	68	30.01283	47	80	33.89481
66	69	30.29767	47	81	33.98778
66	70	30.58317	47	82	34.28000
66	71	30.86942	47	83	34.57300
66	72	31.15639	47	84	34.86644
66	73	31.44407	47	85	35.16047
66	74	31.73244	47	86	35.45500
66	75	32.02140	47	87	35.75000
66	76	32.31110	47	88	36.04543
66	77	32.60133	47	89	36.34170
66	78	32.89248	47	90	36.63825
66	79	33.18467	47	91	36.93520
66	80	33.47620	47	92	37.23279
66	81	33.76801	47	93	37.53075
66	82	34.06235	47	94	37.82916
66	83	34.35824	47	95	38.12802
66	84	34.65568	47	96	38.42730
66	85	34.95463	47	97	38.72701
66	86	35.25413	47	98	39.02713
66	87	35.55716	47	99	39.32764
66	88	35.86367	47	100	39.62854
66	89	36.17360	48	00	39.92984
66	90	36.48614	48	01	40.23141
66	91	36.79929	48	02	40.53325
66	92	37.02430	48	03	40.83536
66	93	37.22335	48	04	41.13773
66	94	37.42235	48	05	41.44036
66	95	37.62235	48	06	41.74325
66	96	37.82235	48	07	42.04639
66	97	38.02235	48	08	42.34968
66	98	38.22235	48	09	42.65312
66	99	38.42235	48	10	42.95671
66	100	38.62235	48	11	43.26045
47	00	38.82235	48	12	43.56434
47	01	39.02235	48	13	43.86838
47	02	39.22235	48	14	44.17257
47	03	39.42235	48	15	44.47691
47	04	39.62235	48	16	44.78140
47	05	39.82235	48	17	45.08604
47	06	40.02235	48	18	45.39083
47	07	40.22235	48	19	45.69577
47	08	40.42235	48	20	46.00086
47	09	40.62235	48	21	46.30610
47	10	40.82235	48	22	46.61149
47	11	41.02235	48	23	46.91703
47	12	41.22235	48	24	47.22272
47	13	41.42235	48	25	47.52856
47	14	41.62235	48	26	47.83455
47	15	41.82235	48	27	48.14069
47	16	42.02235	48	28	48.44698
47	17	42.22235	48	29	48.75342
47	18	42.42235	48	30	49.05999
47	19	42.62235	48	31	49.36670
47	20	42.82235	48	32	49.67355
47	21	43.02235	48	33	49.98054
47	22	43.22235	48	34	50.28767
47	23	43.42235	48	35	50.59494
47	24	43.62235	48	36	50.90234
47	25	43.82235	48	37	51.20987
47	26	44.02235	48	38	51.51754
47	27	44.22235	48	39	51.82534
47	28	44.42235	48	40	52.13327
47	29	44.62235	48	41	52.44134
47	30	44.82235	48	42	52.74954
47	31	45.02235	48	43	53.05787
47	32	45.22235	48	44	53.36634
47	33	45.42235	48	45	53.67494
47	34	45.62235	48	46	53.98367
47	35	45.82235	48	47	54.29254
47	36	46.02235	48	48	54.60154
47	37	46.22235	48	49	54.91067
47	38	46.42235	48	50	55.21994
47	39	46.62235	48	51	55.52934
47	40	46.82235	48	52	55.83887
47	41	47.02235	48	53	56.14854
47	42	47.22235	48	54	56.45834
47	43	47.42235	48	55	56.76827
47	44	47.62235	48	56	57.07834
47	45	47.82235	48	57	57.38854
47	46	48.02235	48	58	57.69887
47	47	48.22235	48	59	58.00934
47	48	48.42235	48	60	58.31994
47	49	48.62235	48	61	58.63067
47	50	48.82235	48	62	58.94154
47	51	49.02235	48	63	59.25254
47	52	49.22235	48	64	59.56367
47	53	49.42235	48	65	59.87494
47	54	49.62235	48	66	60.18634
47	55	49.82235	48	67	60.49787
47	56	50.02235	48	68	60.80954
47	57	50.22235	48	69	61.12134
47	58	50.42235	48	70	61.43327
47	59	50.62235	48	71	61.74534
47	60	50.82235	48	72	62.05754
47	61	51.02235	48	73	62.36987
47	62	51.22235	48	74	62.68234
47	63	51.42235	48	75	62.99494
47	64	51.62235	48	76	63.30767
47	65	51.82235	48	77	63.62054
47	66	52.02235	48	78	63.93354
47	67	52.22235	48	79	64.24667
47	68	52.42235	48	80	64.55994
47	69	52.62235	48	81	64.87334
47	70	52.82235	48	82	65.18687
47	71	53.02235	48	83	65.50054
47	72	53.22235	48	84	65.81434
47	73	53.42235	48	85	66.12827
47	74	53.62235	48	86	66.44234
47	75	53.82235	48	87	66.75654
47	76	54.02235	48	88	67.07087
47	77	54.22235	48	89	67.38534
47	78	54.42235	48	90	67.69994
47	79	54.62235	48	91	68.01467
47	80	54.82235	48	92	68.32954
47	81	55.02235	48	93	68.64454
47	82	55.22235	48	94	68.95967
47	83	55.42235	48	95	69.27494
47	84	55.62235	48	96	69.59034
47	85	55.82235	48	97	69.90587
47	86	56.02235	48	98	70.22154
47	87	56.22235	48	99	70.53734
47	88	56.42235	48	100	70.85327
47	89	56.62235	48	01	71.16934
47	90	56.82235	48	02	71.48554
47	91	57.02235	48	03	71.80187
47	92	57.22235	48	04	72.11834
47	93	57.42235	48	05	72.43494
47	94	57.62235	48	06	72.75167
47	95	57.82235	48	07	73.06854
47	96	58.02235	48	08	73.38554
47	97	58.22235	48	09	73.70267
47	98	58.42235	48	10	74.01994
47	99	58.62235	48	11	74.33734
47	100	58.82235	48	12	74.65487
48	00	59.02235	48	13	74.97254
48	01	59.22235	48	14	75.29034
48	02	59.42235	48	15	75.60827
48	03	59.62235	48	16	75.92634
48	04	59.82235	48	17	76.24454
48	05	60.02235	48	18	76.56287
48	06	60.22235	48	19	76.88134
48	07	60.42235	48	20	77.19994
48	08	60.62235	48	21	77.51867
48	09	60.82235	48	22	77.83754
48	10	61.02235	48	23	78.15654
48	11	61.22235	48	24	78.47567
48	12	61.42235	48	25	78.79494
48	13	61.62235	48	26	79.11434
48	14	61.82235	48	27	79.43387
48	15	62.02235	48	28	79.75354
48	16	62.22235	48	29	80.07334
48	17	62.42235	48	30	80.39327
48	18	62.62235	48	31	80.71334
48	19	62.82235	48	32	81.03354
48	20	63.02235	48	33	81.35387
48	21	63.22235	48	34	81.67434
48	22	63.42235	48	35	81.99494
48	23	63.62235	48	36	82.31567
48	24	63.82235	48	37	82.63654
48	25	64.02235	48	38	82.95754
48	26	64.22235	48	39	83.27867
48	27	64.42235	48	40	83.59994
48	28	64.62235	48	41	83.92134
48	29	64.82235	48	42	84.24287
48	30	65.02235	48	43	84.56454
48	31	65.22235	48	44	84.88634
48	32	65.42235	48	45	85.20827
48	33	65.62235	48	46	85.53034
48	34	65.82235	48	47	85.85254
48	35	66.02235	48	48	86.17487
48	36	66.22235	48	49	86.49734
48	37	66.42235	48	50	86.81994
48	38	66.62235	48	51	87.14267
48	39	66.82235	48	52	87.46554
48	40	67.02235	48	53	87.78854
48	41	67.22235	48	54	88.11167
48	42	67.42235	48	55	88.43494
48	43	67.62235	48	56	88.75834
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48	45	68.02235	48	58	89.40554
48	46	68.22235	48	59	89.72934
48	47	68.42235	48	60	90.05327
48	48	68.62235	48	61	90.37734
48	49	68.82235	48	62	90.70154
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48	51	69.22235	48	64	91.35034
48	52	69.42235	48	65	91.67494
48	53	69.62235	48	66	91.99967
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48	56	70.22235	48	69	92.97467
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48	58	70.62235	48	71	93.62534
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48	60	71.02235	48	73	94.27654
48	61	71.22235	48	74	94.60234
48	62	71.42235	48	75	94.92827
48	63	71.62235	48	76	95.25434
48	64	71.82235	48	77	95.58054
48	65	72.02235	48	78	95.90687
48	66	72.22235	48	79	96.23334
48	67	72.42235	48	80	96.55994
48	68	72.62235	48	81	96.88667
48	69	72.82235	48	82	97.21354
48	70	73.02235	48	83	97.54054
48	71	73.22235	48	84	97.86767
48	72	73			

81	69	31.67188	82	66	36.54967
81	70	31.75178	82	67	36.64682
81	71	32.63249	82	68	37.13693
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81	73	32.89422	82	70	37.71437
81	74	32.67921	82	71	38.00608
81	75	33.10283	82	72	38.29890
81	76	33.44734	82	73	38.59342
81	77	33.73249	82	74	38.88743
81	78	34.01839	82	75	39.18182
81	79	34.30477	82	76	39.47689
81	80	34.59109	82	77	39.77232
81	81	34.87948	82	78	40.06839
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81	85	36.03478	83	82	41.25564
81	86	36.32340	83	83	41.55339
81	87	36.61277	83	84	41.85113
81	88	36.90181	83	85	42.14985
81	89	37.19039	83	86	42.44855
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81	91	37.76626	83	88	43.04589
81	92	38.05319	83	89	43.34454
81	93	38.34029	83	90	43.64319
81	94	38.62746	83	91	43.94184
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81	98	39.77617	83	95	45.13644
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82	83	40.63769	83	98	46.03239
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82	85	41.21204	83	100	46.62969
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82	87	41.78639	84	85	47.22699
82	88	42.07357	84	86	47.52564
82	89	42.36074	84	87	47.82429
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82	91	42.93509	84	89	48.42159
82	92	43.22227	84	90	48.72024
82	93	43.50944	84	91	49.01889
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82	95	44.08379	84	93	49.61619
82	96	44.37097	84	94	49.91484
82	97	44.65814	84	95	50.21349
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82	99	45.23249	84	97	50.81079
82	100	45.51967	84	98	51.10944
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82	102	46.09402	84	100	51.70674
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82	106	47.24272	84	104	52.90132
82	107	47.52989	84	105	53.19997
82	108	47.81707	84	106	53.49862
82	109	48.10424	84	107	53.79727
82	110	48.39142	84	108	54.09592
82	111	48.67859	84	109	54.39457
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82	113	49.25294	84	111	54.99187
82	114	49.54012	84	112	55.29052
82	115	49.82729	84	113	55.58917
82	116	50.11447	84	114	55.88782
82	117	50.40164	84	115	56.18647
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82	120	51.26317	84	118	57.08242
82	121	51.55034	84	119	57.38107
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82	123	52.12469	84	121	57.97837
82	124	52.41187	84	122	58.27702
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82	127	53.27339	84	125	59.17297
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82	131	54.42209	84	129	60.36757
82	132	54.70927	84	130	60.66622
82	133	55.00000	84	131	60.96487
82	134	55.29072	84	132	61.26352
82	135	55.58144	84	133	61.56217
82	136	55.87217	84	134	61.86082
82	137	56.16289	84	135	62.15947
82	138	56.45362	84	136	62.45812
82	139	56.74434	84	137	62.75677
82	140	57.03507	84	138	63.05542
82	141	57.32579	84	139	63.35407
82	142	57.61652	84	140	63.65272
82	143	57.90725	84	141	63.95137
82	144	58.19797	84	142	64.25002
82	145	58.48870	84	143	64.54867
82	146	58.77942	84	144	64.84732
82	147	59.07015	84	145	65.14597
82	148	59.36088	84	146	65.44462
82	149	59.65160	84	147	65.74327
82	150	59.94233	84	148	66.04192
82	151	60.23306	84	149	66.34057
82	152	60.52379	84	150	66.63922
82	153	60.81451	84	151	66.93787
82	154	61.10524	84	152	67.23652
82	155	61.39597	84	153	67.53517
82	156	61.68670	84	154	67.83382
82	157	61.97742	84	155	68.13247
82	158	62.26815	84	156	68.43112
82	159	62.55888	84	157	68.72977
82	160	62.84960	84	158	69.02842
82	161	63.14033	84	159	69.32707
82	162	63.43106	84	160	69.62572
82	163	63.72179	84	161	69.92437
82	164	64.01251	84	162	70.22302
82	165	64.30324	84	163	70.52167
82	166	64.59397	84	164	70.82032
82	167	64.88470	84	165	71.11897
82	168	65.17542	84	166	71.41762
82	169	65.46615	84	167	71.71627
82	170	65.75688	84	168	72.01492
82	171	66.04760	84	169	72.31357
82	172	66.33833	84	170	72.61222
82	173	66.62906	84	171	72.91087
82	174	66.91979	84	172	73.20952
82	175	67.21051	84	173	73.50817
82	176	67.50124	84	174	73.80682
82	177	67.79197	84	175	74.10547
82	178	68.08270	84	176	74.40412
82	179	68.37342	84	177	74.70277
82	180	68.66415	84	178	75.00142
82	181	68.95488	84	179	75.30007
82	182	69.24560	84	180	75.59872
82	183	69.53633	84	181	75.89737
82	184	69.82706	84	182	76.19602
82	185	70.11779	84	183	76.49467
82	186	70.40851	84	184	76.79332
82	187	70.69924	84	185	77.09197
82	188	70.98997	84	186	77.39062
82	189	71.28070	84	187	77.68927
82	190	71.57142	84	188	77.98792
82	191	71.86215	84	189	78.28657
82	192	72.15288	84	190	78.58522
82	193	72.44360	84	191	78.88387
82	194	72.73433	84	192	79.18252
82	195	73.02506	84	193	79.48117
82	196	73.31579	84	194	79.77982
82	197	73.60651	84	195	80.07847
82	198	73.89724	84	196	80.37712
82	199	74.18797	84	197	80.67577
82	200	74.47870	84	198	80.97442
82	201	74.76942	84	199	81.27307
82	202	75.06015	84	200	81.57172
82	203	75.35088	84	201	81.87037
82	204	75.64160	84	202	82.16902
82	205	75.93233	84	203	82.46767
82	206	76.22306	84	204	82.76632
82	207	76.51379	84	205	83.06497
82	208	76.80451	84	206	83.36362
82	209	77.09524	84	207	83.66227
82	210	77.38597	84	208	83.96092
82	211	77.67670	84	209	84.25957
82	212	77.96742	84	210	84.55822
82	213	78.25815	84	211	84.85687
82	214	78.54888	84	212	85.15552
82	215	78.83960	84	213	85.45417
82	216	79.13033	84	214	85.75282
82	217	79.42106	84	215	86.05147
82	218	79.71179	84	216	86.35012
82	219	80.00251	84	217	86.64877
82	220	80.29324	84	218	86.94742
82	221	80.58397	84	219	87.24607
82	222	80.87470	84	220	87.54472
82	223	81.16542	84	221	87.84337
82	224	81.45615	84	222	88.14202
82	225	81.74688	84	223	88.44067
82	226	82.03760	84	224	88.73932
82	227	82.32833	84	225	89.03797
82	228	82.61906	84	226	89.33662
82	229	82.90979	84	227	89.63527
82	230	83.20051	84	228	89.93392
82	231	83.49124	84	229	90.23257
82	232	83.78197	84	230	90.53122
82	233	84.07270	84	231	90.82987
82	234	84.36342	84	232	91.12852
82	235	84.65415	84	233	91.42717
82	236	84.94488	84	234	91.72582
82	237	85.23560	84	235	92.02447
82	238	85.52633	84	236	92.32312
82	239	85.81706	84	237	92.62177
82	240	86.10779	84	238	92.92042
82	241	86.39851	84	239	93.21907
82	242	86.68924	84	240	93.51772
82	243	86.97997	84	241	93.81637
82	244	87.27070	84	242	94.11502
82	245	87.56142	84	243	94.41367
82	246	87.85215	84	244	94.71232
82	247	88.14288	84	245	95.01097
82	248	88.43360	84	246	95.30962
82	249	88.72433	84	247	95.60827
82	250	89.01506	84	248	95.90692
82	251	89.30579	84	249	96.20557
82	252	89.59651	84	250	96.50422
82	253	89.88724	84	251	96.80287
82	254	90.17797	84	252	97.10152
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56	56	40.02983	58	77	35.38811
56	59	41.22283	58	78	35.43889
56	100	41.51630	58	79	35.43641
57	57	39.72484	58	80	35.21845
57	58	39.98699	58	81	35.49884
57	59	39.24830	58	82	35.78113
57	60	39.51284	58	83	37.04847
57	61	39.77604	58	84	37.30641
57	62	31.04239	58	85	37.62999
57	63	31.30913	58	86	37.91429
57	64	31.57682	58	87	38.19983
57	65	31.84889	58	88	38.48446
57	66	32.12544	58	89	38.77640
57	67	32.40613	58	90	39.06700
57	68	32.68774	58	91	39.34426
57	69	32.96826	58	92	39.63199
57	70	33.24864	58	93	39.92826
57	71	33.52782	58	94	40.22000
57	72	33.80363	58	95	40.50842
57	73	34.08096	58	96	40.79828
57	74	34.35869	58	97	41.07864
57	75	34.63821	58	98	41.35951
57	76	34.91849	58	99	41.64000
57	77	35.19884	58	100	41.92269
57	78	35.48031	59	59	36.76749
57	79	35.76281	59	60	31.02873
57	80	36.04630	59	61	31.29100
57	81	36.33090	59	62	31.55413
57	82	36.61677	59	63	31.81904
57	83	36.90389	59	64	32.08489
57	84	37.19227	59	65	32.35116
57	85	37.48190	59	66	32.61871
57	86	37.77281	59	67	32.88723
57	87	37.96894	59	68	33.15670
57	88	38.25528	59	69	33.42709
57	89	38.54282	59	70	33.69838
57	90	38.83169	59	71	33.97055
57	91	39.12174	59	72	34.24384
57	92	39.41305	59	73	34.51745
57	93	39.70569	59	74	34.79215
57	94	39.99956	59	75	35.06783
57	95	40.29466	59	76	35.34483
57	96	40.59099	59	77	35.62399
57	97	40.88856	59	78	35.90460
57	98	41.18844	59	79	36.17794
57	99	41.49063	59	80	36.45461
57	100	41.79512	59	81	36.73410
58	56	39.24617	59	82	37.01725
58	59	39.50741	59	83	37.29459
58	60	39.76979	59	84	37.56900
58	61	31.03320	59	85	37.84328
58	62	31.29788	59	86	38.11685
58	63	31.56348	59	87	38.39047
58	64	31.83014	59	88	38.67180
58	65	32.09781	59	89	38.95093
58	66	32.36648	59	90	39.22855
58	67	32.63606	59	91	39.50721
58	68	32.90659	59	92	39.78591
58	69	33.17804	59	93	40.06442
58	70	33.45038	59	94	40.34380
58	71	33.72369	59	95	40.62387
58	72	33.99786	59	96	41.01100
58	73	34.27284	59	97	41.30142
58	74	34.54857	59	98	41.59106
58	75	34.82470	59	99	41.88199
58	76	35.10284	59	100	42.17381

60	60	31.29882	61	66	38.41821
60	61	31.39000	61	67	38.69723
60	62	31.48128	61	68	38.98007
60	63	31.57274	61	69	39.26343
60	64	31.66423	61	70	39.54729
60	65	31.75571	61	71	40.03194
60	66	31.84710	61	72	40.31707
60	67	31.93863	61	73	40.60277
60	68	32.03033	61	74	40.88902
60	69	32.12227	61	75	41.17583
60	70	32.21461	61	76	41.46317
60	71	34.21878	61	77	41.75104
60	72	34.48078	61	78	42.03943
60	73	34.74361	61	79	42.32833
60	74	35.00729	61	80	42.61773
60	75	35.27179	61	81	42.90760
60	76	35.53706	62	62	32.33149
60	77	35.80316	62	63	32.58270
60	78	36.07009	62	64	32.83490
60	79	36.33787	62	65	33.11420
60	80	36.60660	62	66	33.39663
60	81	36.87630	62	67	33.67904
60	82	37.14682	62	68	33.96426
60	83	37.41803	62	69	34.25151
60	84	37.68981	62	70	34.44899
60	85	38.07783	62	71	34.71877
60	86	38.36823	62	72	34.98874
60	87	38.66325	62	73	35.25950
60	88	38.96388	62	74	35.53127
60	89	39.26112	62	75	35.80379
60	90	39.55894	62	76	36.07711
60	91	39.86130	62	77	36.35123
60	92	40.16727	62	78	36.62613
60	93	40.47593	62	79	36.90179
60	94	40.78614	62	80	37.17819
60	95	40.94069	62	81	37.45833
60	96	41.23604	62	82	37.73310
60	97	41.53284	62	83	38.01174
60	98	41.83170	62	84	38.29084
60	99	42.13249	62	85	38.57063
60	100	42.43470	62	86	38.85146
61	61	31.61016	62	87	39.13264
61	62	31.97137	62	88	39.41454
61	63	32.33264	62	89	39.69701
61	64	32.69794	62	90	39.98010
61	65	33.06140	62	91	40.26379
61	66	33.32683	62	92	40.54800
61	67	33.59322	62	93	40.83290
61	68	33.86054	62	94	41.11831
61	69	34.12880	62	95	41.40430
61	70	34.39807	62	96	41.69079
61	71	34.70813	62	97	41.97764
61	72	35.01899	62	98	42.26341
61	73	35.32877	62	99	42.54949
61	74	35.63716	62	100	42.83609
61	75	35.94348	63	63	32.08263
61	76	36.24886	63	64	32.31463
61	77	36.55344	63	65	32.54688
61	78	36.85826	63	66	32.77928
61	79	37.16334	63	67	33.01183
61	80	37.46869	63	68	33.24453
61	81	37.77434	63	69	33.47738
61	82	38.08029	63	70	33.71038
61	83	38.38654	63	71	33.94353
61	84	38.69309	63	72	34.17683
61	85	39.00004	63	73	34.41028
61	86	39.30729	63	74	34.64388

71	71	37.08389	73	80	39.91374
71	72	37.26474	73	81	40.17987
71	73	37.54653	73	82	40.44700
71	74	37.82832	73	83	40.71450
71	75	38.11011	73	84	40.98200
71	76	38.39190	73	85	41.24950
71	77	38.67369	73	86	41.51700
71	78	38.95548	73	87	41.78450
71	79	39.23727	73	88	42.05200
71	80	39.51906	73	89	42.31950
71	81	39.79985	73	90	42.58700
71	82	40.08164	73	91	42.85450
71	83	40.36343	73	92	43.12200
71	84	40.64522	73	93	43.38950
71	85	40.92701	73	94	43.65700
71	86	41.20880	73	95	43.92450
71	87	41.49059	73	96	44.19200
71	88	41.77238	73	97	44.45950
71	89	42.05417	73	98	44.72700
71	90	42.33596	73	99	45.00000
71	91	42.61775	73	100	45.26750
71	92	42.89954	74	74	39.94879
71	93	43.18133	74	75	39.11662
71	94	43.46312	74	76	39.37973
71	95	43.74491	74	77	39.63780
71	96	44.02670	74	78	39.89587
71	97	44.30849	74	79	40.15394
71	98	44.59028	74	80	40.41201
71	99	44.87207	74	81	40.67008
71	100	45.15386	74	82	40.92815
72	72	37.54653	74	83	41.18622
72	73	37.82832	74	84	41.44429
72	74	38.11011	74	85	41.70236
72	75	38.39190	74	86	41.96043
72	76	38.67369	74	87	42.21850
72	77	38.95548	74	88	42.47657
72	78	39.23727	74	89	42.73464
72	79	39.51906	74	90	42.99271
72	80	39.80085	74	91	43.25078
72	81	40.08264	74	92	43.50885
72	82	40.36443	74	93	43.76692
72	83	40.64622	74	94	44.02499
72	84	40.92801	74	95	44.28306
72	85	41.20980	74	96	44.54113
72	86	41.49159	74	97	44.79920
72	87	41.77338	74	98	45.05727
72	88	42.05517	74	99	45.31534
72	89	42.33696	74	100	45.57341
72	90	42.61875	75	75	39.18082
72	91	42.90054	75	76	39.43889
72	92	43.18233	75	77	39.69696
72	93	43.46412	75	78	39.95503
72	94	43.74591	75	79	40.21310
72	95	44.02770	75	80	40.47117
72	96	44.30949	75	81	40.72924
72	97	44.59128	75	82	40.98731
72	98	44.87307	75	83	41.24538
72	99	45.15486	75	84	41.50345
72	100	45.43665	75	85	41.76152
73	73	38.00430	75	86	42.01959
73	74	38.28609	75	87	42.27766
73	75	38.56788	75	88	42.53573
73	76	38.84967	75	89	42.79380
73	77	39.13146	75	90	43.05187
73	78	39.41325	75	91	43.30994
73	79	39.69504	75	92	43.56801
73	80	39.97683	75	93	43.82608
73	81	40.25862	75	94	44.08415
73	82	40.54041	75	95	44.34222
73	83	40.82220	75	96	44.60029
73	84	41.10399	75	97	44.85836
73	85	41.38578	75	98	45.11643
73	86	41.66757	75	99	45.37450
73	87	41.94936	75	100	45.63257
73	88	42.23115	76	86	43.00000
73	89	42.51294	76	87	43.25807
73	90	42.79473	76	88	43.51614
73	91	43.07652	76	89	43.77421
73	92	43.35831	76	90	44.03228
73	93	43.64010	76	91	44.29035
73	94	43.92189	76	92	44.54842
73	95	44.20368	76	93	44.80649
73	96	44.48547	76	94	45.06456
73	97	44.76726	76	95	45.32263
73	98	45.04905	76	96	45.58070
73	99	45.33084	76	97	45.83877
73	100	45.61263	76	98	46.09684
74	74	39.94879	76	99	46.35491
74	75	39.11662	76	100	46.61298
74	76	39.37973	77	77	40.41201
74	77	39.63780	77	78	40.67008
74	78	39.89587	77	79	40.92815
74	79	40.15394	77	80	41.18622
74	80	40.41201	77	81	41.44429
74	81	40.67008	77	82	41.70236
74	82	40.92815	77	83	41.96043
74	83	41.18622	77	84	42.21850
74	84	41.44429	77	85	42.47657
74	85	41.70236	77	86	42.73464
74	86	41.96043	77	87	42.99271
74	87	42.21850	77	88	43.25078
74	88	42.47657	77	89	43.50885
74	89	42.73464	77	90	43.76692
74	90	42.99271	77	91	44.02499
74	91	43.25078	77	92	44.28306
74	92	43.50885	77	93	44.54113
74	93	43.76692	77	94	44.79920
74	94	44.02499	77	95	45.05727
74	95	44.28306	77	96	45.31534
74	96	44.54113	77	97	45.57341
74	97	44.79920	77	98	45.83148
74	98	45.05727	77	99	46.08955
74	99	45.31534	77	100	46.34762
74	100	45.57341	78	80	43.00000
75	80	43.00000	78	81	43.25807
75	81	43.25807	78	82	43.51614
75	82	43.51614	78	83	43.77421
75	83	43.77421	78	84	44.03228
75	84	44.03228	78	85	44.29035
75	85	44.29035	78	86	44.54842
75	86	44.54842	78	87	44.80649
75	87	44.80649	78	88	45.06456
75	88	45.06456	78	89	45.32263
75	89	45.32263	78	90	45.58070
75	90	45.58070	78	91	45.83877
75	91	45.83877	78	92	46.09684
75	92	46.09684	78	93	46.35491
75	93	46.35491	78	94	46.61298
75	94	46.61298	78	95	46.87105
75	95	46.87105	78	96	47.12912
75	96	47.12912	78	97	47.38719
75	97	47.38719	78	98	47.64526
75	98	47.64526	78	99	47.90333
75	99	47.90333	78	100	48.16140
75	100	48.16140	79	81	43.00000
76	81	43.00000	79	82	43.25807
76	82	43.25807	79	83	43.51614
76	83	43.51614	79	84	43.77421
76	84	43.77421	79	85	44.03228
76	85	44.03228	79	86	44.29035
76	86	44.29035	79	87	44.54842
76	87	44.54842	79	88	44.80649
76	88	44.80649	79	89	45.06456
76	89	45.06456	79	90	45.32263
76	90	45.32263	79	91	45.58070
76	91	45.58070	79	92	45.83877
76	92	45.83877	79	93	46.09684
76	93	46.09684	79	94	46.35491
76	94	46.35491	79	95	46.61298
76	95	46.61298	79	96	46.87105
76	96	46.87105	79	97	47.12912
76	97	47.12912	79	98	47.38719
76	98	47.38719	79	99	47.64526
76	99	47.64526	79	100	47.90333
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77	77	40.41201	80	82	43.25807
77	78	40.67008	80	83	43.51614
77	79	40.92815	80	84	43.77421
77	80	41.18622	80	85	44.03228
77	81	41.44429	80	86	44.29035
77	82	41.70236	80	87	44.54842
77	83	41.96043	80	88	44.80649
77	84	42.21850	80	89	45.06456
77	85	42.47657	80	90	45.32263
77	86	42.73464	80	91	45.58070
77	87	42.99271	80	92	45.83877
77	88	43.25078	80	93	46.09684
77	89	43.50885	80	94	46.35491
77	90	43.76692	80	95	46.61298
77	91	44.02499	80	96	46.87105
77	92	44.28306	80	97	47.12912
77	93	44.54113	80	98	47.38719
77	94	44.79920	80	99	47.64526
77	95	45.05727	80	100	47.90333
77	96	45.31534	81	81	43.00000
77	97	45.57341	81	82	43.25807
77	98	45.83148	81	83	43.51614
77	99	46.08955	81	84	43.77421
77	100	46.34762	81	85	44.03228
78	78	40.92815	81	86	44.29035
78	79	41.18622	81	87	44.54842
78	80	41.44429	81	88	44.80649
78	81	41.70236	81	89	45.06456
78	82	41.96043	81	90	45.32263
78	83	42.21850	81	91	45.58070
78	84	42.47657	81	92	45.83877
78	85	42.73464	81	93	46.09684
78	86	42.99271	81	94	46.35491
78	87	43.25078	81	95	46.61298
78	88	43.50885	81	96	46.87105
78	89	43.76692	81	97	47.12912
78	90	44.02499	81	98	47.38719
78	91	44.28306	81	99	47.64526
78	92	44.54113	81	100	47.90333
78	93	44.79920	82	82	43.00000
78	94	45.05727	82	83	43.25807
78	95	45.31534	82	84	43.51614
78	96	45.57341	82	85	43.77421
78	97	45.83148	82	86	44.03228
78	98	46.08955	82	87	44.29035
78	99	46.34762	82	88	44.54842
78	100	46.60569	82	89	44.80649
79	79	41.44429	82	90	45.06456
79	80	41.70236	82	91	45.32263
79	81	41.96043	82	92	45.58070
79	82	42.21850	82	93	45.83877
79	83	42.47657	82	94	46.09684
79	84	42.73464	82	95	46.35491
79	85	42.99271	82	96	46.61298
79</					

81	99	44.61840	85	99	44.86373
81	91	44.64334	85	87	44.86880
81	88	45.15306	85	88	45.19422
81	83	45.42142	85	89	45.37141
81	84	45.45145	85	90	45.62874
81	85	45.84214	85	91	45.80040
81	86	46.23381	85	92	46.14618
81	87	46.50831	85	93	46.45247
81	89	46.77614	85	94	46.69040
81	90	47.06139	85	95	46.94711
81	100	47.32825	85	96	47.23844
82	82	42.78453	85	97	47.50443
82	83	42.81944	85	98	47.77490
82	84	42.98188	85	99	48.04437
82	85	43.04494	85	100	48.31527
82	86	43.68772	86	86	44.84482
82	87	44.07130	86	87	45.18840
82	88	44.33684	86	88	45.34684
82	89	44.60872	86	89	45.62040
82	90	44.84621	86	90	45.89291
82	91	45.13440	86	91	46.15700
82	92	45.40430	86	92	46.42182
82	93	45.67284	86	93	46.68724
82	94	45.94215	86	94	46.95337
82	95	46.21200	86	95	47.22044
82	96	46.48246	86	96	47.48847
82	97	46.75382	86	97	47.75432
82	98	47.02544	86	98	48.02322
82	99	47.29630	86	99	48.29470
82	100	47.57142	86	100	48.56484
83	83	43.27891	87	87	45.34830
83	84	43.54100	87	88	45.62844
83	85	43.80289	87	89	45.90830
83	86	44.06187	87	90	46.18044
83	87	44.32890	87	91	46.45421
83	88	44.59323	87	92	46.72827
83	89	44.85814	87	93	46.94304
83	90	45.12347	87	94	47.20651
83	91	45.39029	87	95	47.47444
83	92	45.65741	87	96	47.74152
83	93	45.92522	87	97	48.00904
83	94	46.19372	87	98	48.27721
83	95	46.46230	87	99	48.54663
83	96	46.73274	87	100	48.81549
83	97	47.00322	88	88	45.84674
83	98	47.27435	88	89	46.14783
83	99	47.54611	88	90	46.44843
83	100	47.81849	88	91	46.72222
84	84	45.00135	88	92	46.99552
84	85	44.98237	88	93	47.19954
84	86	44.23424	88	94	47.44426
84	87	44.58490	88	95	47.72944
84	88	44.88432	88	96	47.98879
84	89	45.11444	88	97	48.25237
84	90	45.37820	88	98	48.53042
84	91	45.64643	88	99	48.79811
84	92	45.91137	88	100	49.06608
84	93	46.17642	89	89	46.06813
84	94	46.44014	89	90	46.34819
84	95	46.71430	89	91	46.62100
84	96	46.98344	89	92	47.13388
84	97	47.25340	89	93	47.48482
84	98	47.52378	89	94	47.78041
84	99	47.79400	89	95	47.94848
84	100	48.06448	89	96	48.22004
85	85	44.23243	89	97	48.51691
89	89	46.78343	90	90	51.02100
89	90	49.05100	90	100	51.84891
89	100	49.51908	100	100	52.14384
90	80	46.82904			
90	91	47.18994			
90	92	47.45334			
90	93	47.71489			
90	94	47.97612			
90	95	48.24804			
90	96	48.50472			
90	97	48.77208			
90	98	49.03604			
90	99	49.29469			
90	100	49.57890			
91	91	47.48467			
91	92	47.71193			
91	93	47.97372			
91	94	48.23623			
91	95	48.49944			
91	96	48.76334			
91	97	49.02794			
91	98	49.29323			
91	99	49.55817			
91	100	49.82874			
92	92	47.97235			
92	93	48.23330			
92	94	48.49504			
92	95	48.75786			
92	96	49.02071			
92	97	49.28463			
92	98	49.54920			
92	99	49.81442			
92	100	50.08031			
93	93	48.45042			
93	94	48.70467			
93	95	49.01643			
93	96	49.27891			
93	97	49.54287			
93	98	49.80822			
93	99	50.07844			
93	100	50.35042			
94	94	49.61499			
94	95	49.87804			
94	96	49.13784			
94	97	49.39835			
94	98	50.06339			
94	99	50.25720			
94	100	50.59140			
95	95	49.35477			
95	96	49.79741			
95	97	50.08916			
95	98	50.38219			
95	99	50.54470			
95	100	50.84440			
96	96	50.08775			
96	97	50.31879			
96	98	50.56082			
96	99	50.84384			
96	100	51.10463			
97	97	50.87912			
97	98	50.84016			
97	99	51.10180			
97	100	51.36438			
98	98	51.10050			
98	99	51.36153			
98	100	51.62325			

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